

Performance Assessment of a Set of Multi-Objective Optimization Algorithms for Solution of Economic Emission Dispatch Problem

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This paper addresses the realistic economic emission dispatch (EED) problem of power system by considering the operating fuel cost and environmental emission as two conflicting objectives, and power balance and generator limits as two constraints. A novel dynamic multi-objective optimization algorithm, namely the multi-objective differential evolution with recursive distributed constraint handling (MODE-RDC) has been proposed and successfully employed to address this challenging EED problem. It has been thoroughly investigated in two different test cases at three different load demands. The efficiency of the MODE-RDC is also compared with two other multi-objective evolutionary algorithms (MOEAs), namely, the non-dominated sorting genetic algorithm (NSGA-II) and multi-objective particle swarm optimization (MOPSO). Performance evaluation is carried out by comparing the Pareto fronts, computational time and three non-parametric performance metrics. The statistical analysis is also performed, to demonstrate the ascendancy of the proposed MODE-RDC algorithm. Investigation of the performance metrics revealed that the proposed MODE-RDC approach was capable of providing good Pareto solutions while retaining sufficient diversity. It renders a wide opportunity to make a trade-off between operating cost and emission under different challenging constraints.

Povzetek: Opisan je izvorni multi-kriterijski optimirni algoritem za energetske sisteme, ki kombinira kriterij onesnaževanja in kriterij energetske potrošnje.

1 Introduction

The Economic Load Dispatch (ELD) problem deals with the estimation of the scheduled real power generation from the committed units for best economic operation. Over the years the problem has become more complex due to the increasing effects of emissions from fossil fuel based power plants on the environment. The emission and fuel cost of each unit depend on the quantity of power to be generated. Both of them are nonlinear functions of power output. Minimum operating cost does not ensure minimum emission. Each operating condition must satisfy the power balance criterion and should obey the generating limits of the committed units. These can be considered as constraints. Generally, better quality fuel ensures less emission but it can be further reduced by proper scheduling of generation from different units. The cost coefficients and emission coefficients of these generating units do not match. Hence, achieving these two objectives, i.e. less cost and less emission is contradictory in nature. Thus, the EED problem has evolved as a modification of the ELD problem. Therefore, the EED problem is a multi-objective optimization problem with nonlinear constraints.

In [1-2], the power engineers solved the ELD problem by scheduling of the generation of multi-unit

systems using the derivative based Gauss-Siedel and Newton-Raphson algorithms along with the Lagrangian multiplier. These conventional methods suffer from the problem of getting trapped in local minima and also fail for system discontinuities due to prohibited zones. These techniques are inadequate to solve multi-objective problems with nonlinear constraints. Chang et al. [3] rehabilitated the inherently multi-objective EED problem to a single objective one by assigning weights to the operating cost and emission. This weighted sum approach requires many runs of the same algorithm to find the Pareto optimal front. The solutions arrived at by this method do not ensure a uniform Pareto front. The trade-off information is lost when the function is concave. To avoid this bottom-hole different evolutionary based heuristic approaches have been introduced by many researchers [4-5]. These evolutionary algorithms have considered the two objectives simultaneously and are shown to perform better as compared to the conventional ones. Chiang et al. [6] made a further refinement and proposed an improved genetic algorithm to speed up the search process. He used the ϵ -constraint technique for efficient

constraint handling and proposed a multiplier updating mechanism for better exploration of the search space.

Deb et al. [7] proposed the non-dominated sorting genetic algorithm which utilized rank and crowding distance as parameters to arrive at a compromise between the two conflicting objectives. This was applied to the multi-objective environmental economic load dispatch problem in [8]. The Pareto optimal front could be obtained by a single run of the algorithm. But, this population based genetic algorithm depends upon biologically inspired factors like mutation and crossover parameters. It needs further improvement in terms of exploring a wider area in the search space. Brar et al. [9] made improvements in the search space by adding the fuzzy inference system. Muthuswamy et al. [10] modified the non-dominated sorting technique by incorporating a dynamic crowding distance to improve the diversity of solutions in the search space. These algorithms fail when there are discontinuities in the cost function.

Nayak et al. [11] implemented another evolutionary algorithm, the artificial bee colony (ABC) optimization, and improved the convergence rate and reliability under the presence of the prohibited zones and ramp rate limits. Liang et al. [12] modified the ABC algorithm to form an improved artificial bee colony (IABC) by addition of a new skill called chaos ques in the search process. Mori et al. [13] made an excellent improvement in the exploration of search space through the implementation of the particle swarm optimization (PSO) for this multimodal problem. They also used adaptive parameter adjustment to improve the results. A significant improvement in search space exploration was made by Hadji et al. [14]. They incorporated a time varying acceleration of the particles to improve the robustness of the algorithm. Recently, a differential evolution (DE) algorithm came up which generates the next set of population of new particles by the addition of a differential vector obtained from the difference of the position vectors of two different particles other than the particle undergoing evolution [15]. This algorithm is still dependent on the bio-inspired parameters but is able to avoid premature convergence. Meza et al. [16] improved the algorithm by incorporating spherical pruning for better exploitation of the search space. Di et al. [17] introduced a marginal analysis correction operator to improve the constraint handling.

In [18], the particle swarm optimization algorithm has been developed which is based on the intelligence of flock of birds. The same has been improved and tested for multi-objective problems in [19-21]. The EED problem has been solved to decide the unit commitment of the power system by considering operational power flow and environmental constraints in [22]. But, it again utilized the method of conversion of the multi-objective problem to a single objective one. A new approach to optimization is proposed in [23] which hybridized adaptive PSO and DE for improvement of the search space. An improvement over ABC called as multi-objective global best artificial bee colony (MOGABC) optimization is suggested in [24] for better constraint

handling in EED problem. The EED problem has been further modified and applied to the micro-grid containing renewable sources along with the conventional thermal power stations in [25]. It also converts the problem to a single objective one by incorporating a h-index.

In this paper, a new constraint handling mechanism has been implemented, and a new multi-objective optimization (MOP) algorithm, namely the multi-objective differential evolution with recursive distributed constraint handling (MODE-RDC) has been proposed. The constraint handling mechanism is suitably incorporated in three multi-objective optimization (MOP) algorithms, and the effectiveness of the algorithms has been tested under various load conditions.

2 Multi-objective optimization: a review

The main aim of the multi-objective optimization technique is to optimize two or more conflicting objectives simultaneously. The MOP is denoted by a decision variable vector, each element of which represents the objective functions [21]. The solution to the MOP is the optimum value of the vector function by considering all the constraints. A multi-objective minimization problem can be generalized as follows:

$$\text{Minimize } f(\vec{x}) = (f_1(\vec{x}), f_2(\vec{x}), \dots, f_M(\vec{x})) \quad (1)$$

Subject to constraints:

$$g_j(\vec{x}) \leq 0; j=1, 2, \dots, J \quad (2)$$

$$h_k(\vec{x}) = 0; k=1, 2, \dots, K \quad (3)$$

where, \vec{x} is a vector with N decision variables

$$\vec{x} = [x_1, x_2, \dots, x_N]^T$$

The search space may be limited by lower and upper bounds

$$lb_i \leq x_i \leq ub_i; i=1, 2, \dots, N \quad (4)$$

A solution vector $\vec{u} = [u_1, u_2, \dots, u_N]^T$ dominates over another solution $\vec{v} = [v_1, v_2, \dots, v_N]^T$ if and only if

$$\left. \begin{aligned} f_i(\vec{u}) &\leq f_i(\vec{v}) \forall i \in [1, 2, \dots, M] \\ f_i(\vec{u}) &< f_i(\vec{v}) \text{ for at least one } i \in [1, 2, \dots, M] \end{aligned} \right\} \quad (5)$$

Solutions that are not dominated by other solutions within the given solution space are said to be non-dominated solutions. The front obtained by mapping such points onto the objective space is said to be the Pareto optimal front (POF)

$$\text{POF} = f(\vec{x}) = \{ \{f_1(\vec{x}), f_2(\vec{x}), \dots, f_k(\vec{x})\}; |\vec{x} \in p \} \quad (6)$$

where, p is the set of non-dominated particles.

3 Economic emission dispatch problem

The generation schedule for minimum operating cost is called ELD. This schedule is obtained when the committed units of the power system are able to supply the load demanded and the associated transmission losses by satisfying the generator limits. The thermal generating units are associated with emissions which are highly polluting in nature. Therefore, it is essential to minimize

the emissions along with the fuel cost. The problem has been transformed to EED problem. It is considered as a multi-objective optimization problem as minimum operating cost does not ensure minimum emission [5]. The operating cost of thermal power systems depends mostly on the cost of fuel used. The quantity of fuel used by each unit depends on the generated power, efficiency of turbine etc.

The fuel cost characteristics of the generating units are normally of the second order polynomial of the generated power. Thus, the operating fuel cost of the i th generator supplying a real power P_{Gi} is given by

$$F_i = a_i P_{Gi}^2 + b_i P_{Gi} + c_i \tag{7}$$

where, a_i , b_i and c_i are the coefficients of cost function.

The emission from the generator i can be approximated as

$$E_i = \alpha_i + \beta_i P_{Gi} + \gamma_i P_{Gi}^2 \tag{8}$$

where, α_i , β_i , γ_i are the coefficients of emission function.

The aim of the ELD problem is to determine generation schedule for the minimum total fuel cost given by

$$F_T = \sum_{i=1}^N F_i \tag{9}$$

subject to the constraints.

The total real power generation must be equal to the demand plus transmission losses

$$\sum_{i=1}^N P_{Gi} = P_D + P_L \tag{10}$$

where, P_D is the load demand on the system and P_L is the transmission loss. It is given by Kron’s formula

$$P_L = \sum_{i=1}^N \sum_{j=1}^N P_{Gi} B_{ij} P_{Gj} + \sum_{i=1}^N B_{i0} P_{Gi} + B_{00}. \tag{11}$$

The constants B_{ij} , B_{i0} and B_{00} are dependent on the line parameters. The generated real power of each unit must be within the feasible lower and upper bounds.

$$P_{Gi(\min)} \leq P_{Gi} \leq P_{Gi(\max)}; i = 1, 2, \dots, N. \tag{12}$$

Thus, the sole objective of the EED problem is to optimize both the fuel cost and emission simultaneously. Hence, it is inherently a multi-objective optimization problem where these two objectives which are conflicting in nature need to be optimized. The set of all the potential compromised solutions is represented by the Pareto optimal front.

The problem can be stated as:

$$\text{minimize}_{P_G} [F_T(P_G), E_T(P_G)] \tag{13}$$

$$\text{Subject to: } g(P_G) = 0; h(P_G) \leq 0$$

where, the equality constraint is represented by equation (14) and inequality constraint by equation (15).

$$\sum_{i=1}^N P_{Gi} - P_D - P_L = 0 \tag{14}$$

$$P_{Gi} - P_{Gi}^{\max} \leq 0; P_{Gi}^{\min} - P_{Gi} \leq 0 \tag{15}$$

4 Multi-objective optimization algorithms

The multi-objective evolutionary algorithms can be categorized mostly into four types in accordance with the algorithmic framework, such as indicator based, convolution based, memetic based and non-dominated

sorting based. In this paper, we have solved the economic emission dispatch problem using three different multi-objective optimization algorithms that are based on non-dominated sorting.

4.1 Non-dominated Sorting Genetic Algorithm-II (NSGA-II)

This algorithm was formulated by Deb et al. [7], [8] for solving the multi-objective optimization problems. It is initialized with a random population, and used some operators for covering the objective space uniformly on the Pareto set. For multi-criteria optimization it uses three strategies: non-domination sorting, ranking based on density and crowding comparison. The individuals are classified into several layers based on their rank and crowding distance. The diversity in the solutions is maintained by rejecting the solutions with lower crowding distance. The quality of solutions is ensured by selecting the individuals with lower ranks. The advantage of this algorithm is that the complexity of computation is lowered and elitism is maintained.

4.2 Non-dominated Sorting Multi-Objective Particle Swarm Optimization (NS-MOPSO)

Kennedy and Eberhart proposed that any optimization problem can be solved by mimicking the movement of a flock of birds and school of fish [18]. The social behavior of the swarm is to change their position and velocity to maximize their chance of getting food and follow the best successful neighbor. This lead to the formulation of particle swarm optimization (PSO). In this method of optimization, a local best and a global best solution are identified. The i^{th} particle in the population having the best position (pbest) may be represented by p_i , that gives the best fitness value represented as

$$p_i = (p_{i1}, p_{i2}, \dots, p_{iN}) \tag{16}$$

The old and new velocity of the particles will be shown in equation (17) and (18) respectively.

$$V_i = (v_{i1}, v_{i2}, \dots, v_{iN}) \tag{17}$$

$$v_{id}(t) = wv_{id}(t-1) + c_1 r_1 (p_{id} - x_{id})(t-1) + c_2 r_2 (p_{id} - x_{id})(t-1) \tag{18}$$

and the new position of the particle will be

$$x_{id}(t) = x_{id}(t-1) + \chi v_{id}(t) \tag{19}$$

where, $d = 1, 2, \dots, D$ is the dimension of the decision variables and $i = 1, 2, \dots, N$, and χ is the constriction factor which constricts and controls the velocity magnitude. w , c_1 and c_2 are weight parameters and r_1 , r_2 are random numbers known as acceleration constants in the range [0, 1]. This method of improvement of position and velocity is applied to the non-dominating vectors to solve the multi-objective problem [14], [19] & [20].

4.3 Multi-Objective Differential Evolution with Recursive Distributed Constraint handling (MODE-RDC)

The differential evolution (DE) algorithm as developed by Stern and Price [15] is less dependent on bio-inspired mechanisms, and serves better for multivariable problems. The multi-objective optimization using differential evolution (MODE) proposed by Meza et al. [16] is an improvement of DE to solve multiple number of conflicting objectives simultaneously. The MODE is an evolutionary multi-objective optimization algorithm that retains the diversity of solutions on the Pareto front. This real coded stochastic algorithm uses an initial population to explore the search space by avoiding convergence to local optimal points. It uses two main operators: mutation and cross over. Each initial particle of the population is improved using these two operators. The mutation operator uses a differential vector selected from the particles other than the target particle. Three vectors $x_{r0,g}$, $x_{r1,g}$ and $x_{r2,g}$ are selected randomly from the population and the first one is updated with the difference of the other two. It is done as follows:

$$v_{i,g} = x_{r0,g} + F \cdot (x_{r1,g} - x_{r2,g}) \tag{20}$$

where, $v_{i,g}$ is the mutant vector created from the target vector $x_{r0,g}$ and $x_{r1,g}$, $x_{r2,g}$ are two other vectors; $F \in (0,1+)$ is the scale factor that controls the rate of evolution.

A new trial vector (child) is created from the mutant vector and the target vector after cross over.

$$u_{i,g} = u_{j,i,g} = \begin{cases} v_{j,i,g} & \text{if } (\text{rand}_j(0,1) \leq C_r \text{ or } j = j_{\text{rand}}) \\ x_{j,i,g} & \text{otherwise} \end{cases} \tag{21}$$

where, the cross over probability $C_r \in [0,1]$. The child and the parent are tested for their fitness. The one with the best fitness is selected for participation in the next generation.

$$x_{i,g+1} = \begin{cases} u_{i,g} & \text{if } f(u_{i,g}) \leq f(x_{i,g}) \\ x_{i,g} & \text{otherwise} \end{cases} \tag{22}$$

This is done for all $i=1, 2, \dots, n$ where $n =$ population size. The steps of the proposed MODE-RDC algorithm are summarized as follows:

- I. Initialize the number of individuals N and the population $P(0)$ by random selection within the limits of the search space. Set the fitness function, constraints, maximum number of generations, mutation factor, cross over rate and tolerance.
- II. Evaluate $P(0)$ using the fitness function and constraint
- III. If constraint violation is out of bounds call the recursive distributed constraint handler
- IV. Obtain the non-dominated solutions in $P(0)$ and store in $D(0)$
- V. Update the populations till the maximum number of generations or the convergence criterion is reached
 1. Randomly select a subpopulation of $N_s(k)$ with the proposed solution on $P(k)$
 2. Apply the DE operators on $N_s(k)$ to get the offspring $O(k)$:

- a) Perform the mutation operation.
- b) Apply the fixing rule for boundary constraint violations.
- c) Perform cross over operation.
3. Evaluate offspring $O(k)$ and determine constraint violations
4. Call the recursive distributed constraint handler until constraint violation is within tolerable limits
5. Compare the parent and offspring and select the best store in $D(k)$
6. Apply dominance,
- VI. Modify $D(k)$, perform non dominated sorting on $D(k)$ and plot the Pareto front. Terminate the algorithm. Select the proper solution using the high level decision making rules. Here, we have used the allowable emission norms as the accepted solution.

4.3.1 Constraint handling

The main problem in finding the solution to the EED problem is that every new population evolved must satisfy the upper and lower bounds along with the nonlinear power balance constraint. The power balance constraint, being a polynomial of the individual solutions, makes it a complicated task to ensure convergence. Therefore, a continuous effort has to be made to restrict the solutions in the feasible area. Here, we propose a recursive distributed constraint handling method. The constraint c is the mismatch of power defined as

$$c = \sum_{i=1}^N P_{Gi} - P_D - P_L \tag{23}$$

if $c \leq \epsilon$, then $P_{Gi} = P_{Gi}$

$$\text{else } P_{Gi} = P_{Gi} - \frac{|c|}{N}$$

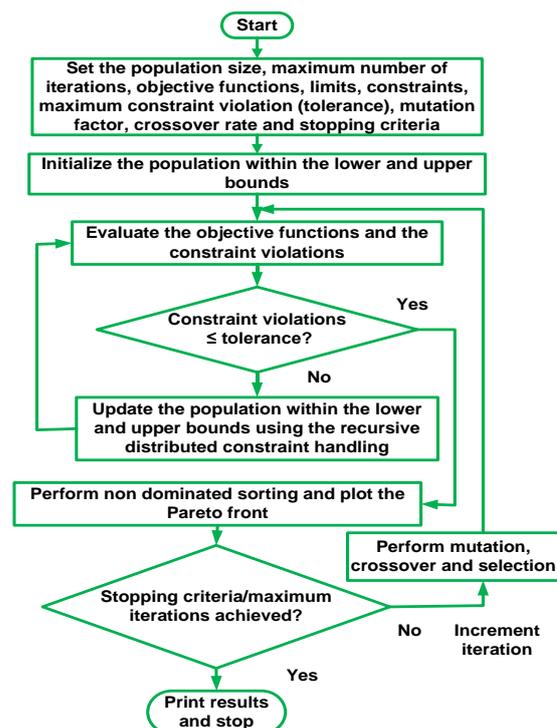


Figure 1: Flowchart of MODE-RDC algorithm.

$$\text{subject to } P_{Gi}^{\min} \leq P_{Gi} \leq P_{Gi}^{\max}$$

where, ϵ is the maximum allowable constraint violation. The constraint violation is evaluated and distributed over the decision variables. The values of the N decision variables will change until the constraint violation is restricted within the permissible limits. Thus the solutions are confined within the feasible work space.

The proposed algorithm is implemented using sequences shown in the flowchart (fig. 1). In the first block, the parameters including the limits are set. The second block initializes the population randomly between the upper and lower limits of the generating units. The population created is evaluated for the constraint violation; if the violation is high, then the population is updated using the constraint handler. The non-dominated sorting is performed, and Pareto optimal front is plotted from the updated population. This population represents the first iteration; subsequent iterations are performed to get further modified populations by applying equations (20), (21) and (22). This process is continued till convergence or the maximum number of iterations performed.

5 Performance measures

The following three performance metrics [21] have been applied to investigate the performance quality of the non-dominated solutions obtained in the form of Pareto fronts using different algorithms.

5.1 Generation Distance (GD)

It is the estimated distance between the non-dominated solution vectors from the standard efficient front. It is mathematically expressed as

$$GD = \frac{\sqrt{\sum_{i=1}^n d_i^2}}{n} \tag{24}$$

where, n is the number of solution vectors and d_i is the minimum Euclidean distance between each of them. $GD=0$ indicates that all the solution vectors are present in the standard Pareto front. A smaller positive value of GD means the Pareto front obtained from the proposed algorithm is closer to the standard Pareto front.

5.2 Spacing (S)

Spacing is the measure of the spread of the solution vectors. It is expressed as

$$S \triangleq \sqrt{\frac{1}{n-1} \sum_{i=1}^n (\bar{d} - d_i)^2} \tag{25}$$

where, $d_i = \min_j (|f_1^i(\vec{x}) - f_1^j(\vec{x})| + |f_2^i(\vec{x}) - f_2^j(\vec{x})|)$ for all $i, j = 1, 2, \dots, n$ and \bar{d} = mean of all d_i and n is the number of non-dominated solution vectors found so far. The lower the value of S the better is the Pareto solution.

5.3 Diversity metric (Δ)

It measures how evenly the solution vectors are distributed in the search space, i.e. extent of the spread on the Pareto front. It is found from the Euclidean distances as follows

$$\Delta = \frac{d_f + d_l + \sum_{i=1}^{N-1} |d_i - \bar{d}|}{d_f + d_l + (n-1)\bar{d}} \tag{26}$$

where, d_i is the distance between the consecutive solution vectors in the non-dominated solution set. The average of these distances is \bar{d} . Here, d_f and d_l are the first and last Euclidean distances. A low value of Δ indicates better diversity, and $\Delta=0$ means the non-dominated solution vectors are uniformly spread on the Pareto front.

6 Simulation study and results

The EED problem was simulated for two different standard test cases i.e., IEEE 14 bus and IEEE 30 bus. The system data of these two test cases were obtained from the website www.ee.washington.edu/research/pstca. The cost and emission coefficients were also recorded from standard sources [22] and are presented in the Appendix along with the B coefficients. Each test case is solved for three different load demands. The solutions are obtained by applying three different algorithms e.g., NSGA-II, MOPSO and proposed MODE-RDC. The algorithms are run in a MATLAB environment with a PC running on Microsoft windows 8 platform having a core i3 processor with a clock speed of 1.3 GHz and RAM of 4 GB. A maximum generation of 300 is taken with a population size of 100. The crossover rate is chosen as intermediate with the ratio set as 1.2 and mutation chosen as Gaussian with a scale of 0.1 and a shrink of 0.5 for NSGA-II. The velocity weight of MOPSO is selected as 0.4 and position weights as 1 with a population size of 100 and a maximum number of iterations of 100. The scaling factor of differential evolution is set as 0.5 and crossover rate as 0.5 with a population size of 100.

6.1 Test case I: IEEE-14 bus system

The algorithms were applied to this test case for three different load demands; i.e., for 200 MW, 259 MW and 300 MW. The performance was compared with respect to Pareto optimal front, computational time, fuel cost, transmission loss involved and statistical performance metrics.

6.1.1 IEEE-14 bus system: load demand 200 MW

The Pareto optimal fronts obtained by applying the three algorithms are compared and shown in Fig.2 for a load demand of 200MW.

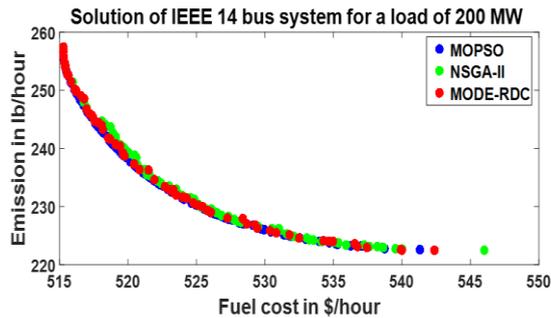


Figure 2: Solution of IEEE 14 bus system for a load demand of 200 MW.

Algorithm	NSGA-II	MOPSO	MODE-RDC
PG1 (MW)	121.894	117.4404	121.1744
PG2 (MW)	37.4252	41.0169	41.8528
PG3 (MW)	19.3125	19.9156	20.4068
PG4 (MW)	10.0000	13.9457	10.9482
PG5 (MW)	15.6575	11.8954	10.0000
Time (sec)	85.4620	0.963873	9.0003
PL (MW)	4.2892	4.2230	4.3822
Fuel Cost (\$/hour)	518.569	518.6977	518.3990
Emission(lb/hour)	244.963	241.1887	242.3576

Table 1: Results of EED of IEEE 14 bus system for a load demand of 200 MW.

Algorithm		NSGA-II	MOPSO	MODE-RDC
Generation Distance (GD)	Minimum	0.0452	0.0714	0.0273
	Maximum	0.0819	0.0714	0.0772
	Average	0.051075	0.0714	0.050145
	Standard Deviation	0.0144013	0.0000	0.0059599
Spacing (S)	Minimum	0.2266	0.5864	0.2659
	Maximum	0.7777	0.5864	0.5576
	Average	0.469715	0.5864	0.37959
	Standard Deviation	0.135470	0.0000	0.0643687
Diversity (A)	Minimum	1.2497	0.7446	0.4843
	Maximum	1.6853	0.7446	0.7300
	Average	1.47758	0.7446	0.613785
	Standard Deviation	0.134289	0.0000	0.0710588

Table 2: Performance of algorithms for IEEE 14 bus system at load demand of 200 MW.

The comparative generation schedule, fuel cost, emission and transmission loss are presented in Table 1. The Pareto front obtained by applying the proposed MODE-RDC algorithm and other two algorithms for different load conditions are depicted from Fig.2 to Fig. 7. The fuel cost value (518.399\$/hour) obtained is lowest among all the three competitive algorithms. The emission obtained from the proposed algorithm is also comparable with other two. Similarly, the algorithms were run for 25 times, and the performance metrics were calculated which are presented in Table 2. The average spacing obtained is 0.37959 which is the lowest among all the three algorithms. The average values of other two

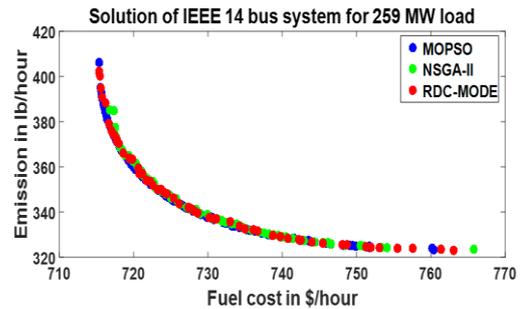


Figure 3: Solution of IEEE 14 bus system for a load demand of 259 MW.

Algorithm	NSGA-II	MOPSO	MODE-RDC
PG1 (MW)	150.416	150.6611	130.7742
PG2 (MW)	51.3048	50.2912	53.0186
PG3 (MW)	23.5338	23.7902	26.3320
PG4 (MW)	23.5837	22.8592	30.7226
PG5 (MW)	17.29	18.3925	24.2551
Time (sec)	91.4121	2.380883	8.0020
PL (MW)	7.1283	6.9942	6.1025
Fuel Cost (\$/hour)	720.3	720.1619	720.1591
Emission (lb/hour)	360	359.2373	359.1248

Table 3: Results of EED for IEEE 14 bus system at load demand of 259 MW.

Algorithm		NSGA-II	MOPSO	MODE-RDC
Generation Distance (GD)	Minimum	0.061130	0.1056	0.056818
	Maximum	0.247369	0.1056	0.215051
	Average	0.115768	0.1056	0.094455
	Standard Deviation	0.052146	0.0000	0.037827
Spacing (S)	Minimum	0.531774	0.6438	0.527058
	Maximum	2.442706	0.6438	1.926600
	Average	1.099879	0.6438	0.641592
	Standard Deviation	0.528886	0.0000	0.428131
Diversity (A)	Minimum	1.200668	0.5898	0.526846
	Maximum	1.702898	0.5898	0.825663
	Average	1.456543	0.5898	0.569785
	Standard Deviation	0.124752	0.0000	0.077072

Table 4: Performance of algorithms for IEEE 14 bus system at load demand of 259 MW.

performance matrices show improved performance of the proposed algorithm. This indicates that the Pareto solutions obtained by the proposed algorithm are superior to the competing algorithms.

6.1.2 IEEE-14 bus system: load demand 259 MW

Figure 3 shows the Pareto optimal fronts obtained for the test case with the load demand of 259 MW.

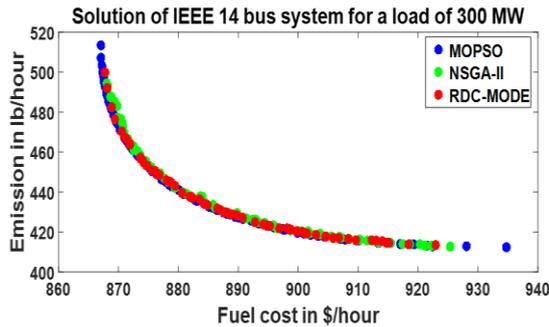


Figure 4: Solution of IEEE 14 bus system for a load demand of 300 MW.

Algorithm	NSGA-II	MOPSO	MODE-RDC
PG1 (MW)	158.385	159.5448	144.5312
PG2 (MW)	59.5374	57.2405	61.6878
PG3 (MW)	28.554	29.1715	30.9264
PG4 (MW)	34.3464	36.9012	41.7176
PG5 (MW)	27.8335	26.9604	29.1517
Time (sec)	94.0921	2.303318	8.0025
PL (MW)	8.6563	9.8184	8.0147
Fuel Cost (\$/hour)	880.909	879.916	880.4091
Emission (lb/hour)	440.116	440.862	440.234

Table 5: Results of EED of IEEE 14 bus system for load demand of 300 MW.

Algorithm		NSGA-II	MOPSO	MODE-RDC
Generation Distance (GD)	Minimum	0.056728	0.1245	0.055189
	Maximum	0.216685	0.1245	0.345505
	Average	0.123737	0.1245	0.120521
	Standard Deviation	0.044166	0.0000	0.058929
Spacing (S)	Minimum	0.510125	0.7691	0.568051
	Maximum	2.065131	0.7691	1.644507
	Average	1.154852	0.7691	0.764450
	Standard Deviation	0.428284	0.0000	0.666390
Diversity (Δ)	Minimum	1.269374	0.6529	0.491511
	Maximum	1.580342	0.6529	0.964161
	Average	1.426765	0.6529	0.648467
	Standard Deviation	0.087880	0.0000	0.102660

Table 6: Performance of algorithms for IEEE 14 bus system at load demand of 300 MW.

The generation schedule for this load is presented in Table 3, and the statistical performance metric values are shown in Table 4. The values of fuel cost and emission obtained by the proposed algorithm are better as compared to the other two algorithms. The generation schedule obtained by the former leads to less transmission loss. The proposed MODE-RDC algorithm shows lower average values of GD, S and Δ as compared to the other two competitive algorithms.

6.1.3 IEEE-14 bus system: load demand 300 MW

With a higher load of 300 MW the Pareto optimal fronts obtained using the algorithms are shown in Fig. 4.

Load (MW)	Algorithm	MODE-RDC Wins	MODE-RDC Losses	Detected differences
200	NSGA-II	17	8	$\alpha = 0.1$
	MOPSO	13	12	-
259	NSGA-II	18	7	$\alpha = 0.5$
	MOPSO	13	12	-
300	NSGA-II	18	7	$\alpha = 0.5$
	MOPSO	13	12	-

Table 7: Result of sign test on MODE-RDC algorithm for IEEE 14 bus system with GD metric as winning parameter.

Load (MW)	Algorithm	MODE-RDC Wins	MODE-RDC Losses	Detected differences
200	NSGA-II	14	11	-
	MOPSO	13	12	-
259	NSGA-II	16	9	-
	MOPSO	13	12	-
300	NSGA-II	14	11	-
	MOPSO	13	12	-

Table 8: Result of sign test on MODE-RDC algorithm for IEEE 14 bus system with S metric as winning parameter.

The generation schedule and performance metrics of the solution points are presented in Tables 5 and 6 respectively. The fuel cost and emission obtained using proposed MODE-RDC algorithm is better in terms of emission and PL in MW. The transmission losses involved due to the schedule obtained by the proposed algorithm is also lower. The average value of GD, S and Δ metrics of the solutions arrived from the proposed algorithm are less than that of the other two. Thus the quality of solutions is maintained.

6.1.4 IEEE-14 bus system: summary of results

The summary of generation schedules obtained for the three load conditions using the three algorithms as presented in Tables 1, 3 and 5 show that the fuel cost for the proposed algorithm provides improved performance for the load conditions. For the IEEE 14 bus test case, the two-tailed Sign tests [21] is conducted for the pair-wise comparison of the algorithms by considering three different performance metrics, and are presented in Tables 7, 8 and 9. The tests were carried out for all the three load conditions and by repeated run of the three algorithms for 25 times. It is observed from Tables 7, 8 and 9 that the proposed algorithm wins over the other two for all loads in terms of all the three performance metrics i.e. the generation distance, spacing and diversity metric as winning parameters. It can be pointed in Table-10 that in Sign test, if more than 17 wins are recorded, then the algorithm is better with a detected difference $\alpha=0.1$; and if more than 18 wins are recorded then, $\alpha=0.05$.

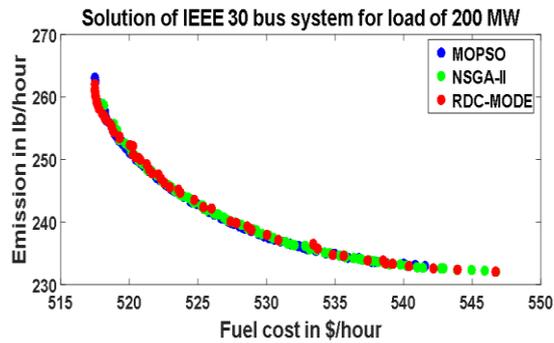


Figure 5: Solution of IEEE 30 bus system for load demand of 200 MW.

Load (MW)	Algorithm	MODE-RDC Wins	MODE-RDC Losses	Detected differences
200	NSGA-II	25	0	0.05
	MOPSO	13	12	-
259	NSGA-II	25	0	0.05
	MOPSO	13	12	-
300	NSGA-II	25	0	0.05
	MOPSO	13	12	-

Table 9: Result of sign test on MODE-RDC algorithm for IEEE 14 bus system with Δ metric as winning parameter.

No. of algorithm runs	$\alpha = 0.05$	$\alpha = 0.1$
5	5	5
6	6	6
7	7	6
8	7	7
9	8	7
10	9	8
11	9	9
12	10	9
13	10	10
14	11	10
15	12	11
16	12	12
17	13	12
18	13	13
19	14	13
20	15	14
21	15	14
22	16	15
23	17	16
24	18	16
25	18	17

Table 10: Significant values for decision on two-tailed sign test.

It is evident from the Table 7 and 8 that the proposed MODE-RDC algorithm shows better performance as compared to other two competitive algorithms. The algorithm is better with respect to NSGA-II a detected difference $\alpha=0.1$ for load of 200 MW, and a detected difference of $\alpha=0.05$ for load of 259MW and 300 MW. However, the proposed algorithm does not show much improvement as compared to MOPSO algorithm.

6.2 Test case II: IEEE-30 bus system

The algorithms were applied to this test case for three different load demands; i.e., for 200 MW, 283.4 MW and

Algorithm	NSGA-II	MOPSO	MODE-RDC
PG1 (MW)	103.927	104.4705	100.8991
PG2 (MW)	37.512	37.7012	41.8153
PG3 (MW)	18.996	19.3131	19.4211
PG4 (MW)	18.718	16.8090	14.9330
PG5 (MW)	13.021	12.7445	14.9143
PG6 (MW)	12.000	12.9950	12.0000
Time (sec)	90.8698	1.5908	8.0285
PL (MW)	4.1740	4.0333	3.9828
Fuel Cost (\$/hour)	524.966	523.9469	523.7250
Emission (lb/hour)	244.007	244.0324	244.9227

Table 11: Results of EED of IEEE 30 bus system for a load demand of 200 MW.

Algorithm		NSGA-II	MOPSO	MODE-RDC
Generation Distance (GD)	Minimum	0.018414	0.0457	0.013645
	Maximum	0.088774	0.0457	0.094384
	Average	0.034309	0.0457	0.032455
	Standard Deviation	0.015609	0.0000	0.009311
Spacing (S)	Minimum	0.159507	0.2623	0.156047
	Maximum	0.870246	0.2623	0.807493
	Average	0.304470	0.2623	0.255573
	Standard Deviation	0.157360	0.0000	0.099082
Diversity (Δ)	Minimum	0.975386	0.5672	0.547595
	Maximum	1.575610	0.5672	0.853479
	Average	1.223858	0.5672	0.558198
	Standard Deviation	0.173773	0.0000	0.052061

Table 12: Performance of algorithms for IEEE 30 bus system at load demand of 200 MW.

Algorithm	NSGA-II	MOPSO	MODE-RDC
PG1 (MW)	132.672	134.7225	111.077
PG2 (MW)	53.443	50.2415	51.679
PG3 (MW)	27.719	27.0213	31.856
PG4 (MW)	29.870	31.4431	33.083
PG5 (MW)	25.102	23.0641	30.000
PG6 (MW)	21.916	24.2446	31.969
Time (sec)	94.5415	2.0302	8.003
PL (MW)	7.32	7.3371	6.264
Fuel Cost (\$/hour)	821.269	820.1034	822.0048
Emission (lb/hour)	380.213	380.7899	379.5462

Table 13: Results of EED of IEEE 30 bus system for a load demand of 283.4 MW.

350 MW. The performance is compared with respect to Pareto optimal front, computational time, fuel cost, transmission loss involved and statistical performance metrics.

6.2.1 IEEE-30 bus system: load demand 200 MW

The Pareto optimal fronts obtained by applying the three algorithms for the load demand of 200 MW are presented in Figure 5.

From the simulation output it reveals that the Pareto curve obtained by applying the proposed algorithm covers a wider area of the search space. The generation

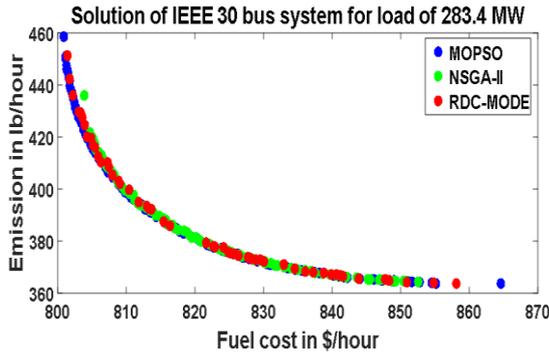


Figure 6: Solution of IEEE 30 bus system for load demand of 283.4 MW.

schedule for an acceptable emission level is achieved, and is presented in Table 11.

The quality of solutions is assessed by evaluating all the three performance metrics, and is presented in Table 12. The cost of fuel obtained by employing the proposed algorithm is lower, and the corresponding schedule causes lower transmission loss. It surpasses the performance of NSGA-II in terms of computational time. The lower average values of all the three performance matrices imply superior performance of the proposed algorithm over other two.

6.2.2 IEEE-30 bus system: load demand 283.4 MW

The test case is subjected to the rated load of 283.4 MW, and performance of the algorithms is assessed. The Pareto fronts obtained for this demand are presented in Figure 6.

The Pareto curve corresponding to the proposed algorithm covers a wide area of the search space. The generation schedules obtained by applying the algorithms are shown in Table 13. The proposed algorithm yields lower values of fuel cost and emission. The transmission losses involved with this schedule is less than the other two algorithms. The quality of solutions is assessed by running the algorithms for 25 times; statistical values of the performance metrics thus obtained are presented in Table 14. The average diversity of the solutions using the proposed algorithm is less than that of the other two algorithms. It also requires less computational time as compared to the NSGA-II.

6.2.3 IEEE-30 bus system: load demand 350 MW

The test case is further subjected to a higher load of 350 MW, and performance of the algorithms is assessed. The Pareto optimal fronts are shown in Figure 7. The generating schedule for the system obtained for this demand is presented in Table 15.

The statistical behavior of the performance metrics obtained for the solutions are shown in Table 16. It is observed that the proposed algorithm performs better than NSGA-II in terms of diversity of solutions, computational time, fuel cost and emission values.

Algorithm		NSGA-II	MOPSO	MODE-RDC
Generation Distance (GD)	Minimum	0.054373	0.1407	0.021384
	Maximum	0.116501	0.1407	0.233931
	Average	0.077291	0.1407	0.065103
	Standard Deviation	0.017481	0.0000	0.029863
Spacing (S)	Minimum	0.383454	0.9516	0.339348
	Maximum	1.026579	0.9516	2.075391
	Average	0.621816	0.9516	0.621204
	Standard Deviation	0.189580	0.0000	0.360044
Diversity (A)	Minimum	0.603026	0.6719	0.563586
	Maximum	1.229024	0.6719	0.767057
	Average	0.968746	0.6719	0.670803
	Standard Deviation	0.163341	0.0000	0.066364

Table 14: Performance of algorithms for IEEE 30 bus system at load demand of 283.4 MW.

Algorithm	NSGA-II	MOPSO	MODE-RDC
PG1 (MW)	159.003	163.500	162.974
PG2 (MW)	68.918	66.800	65.864
PG3 (MW)	46.060	32.600	36.256
PG4 (MW)	25.070	35.000	33.083
PG5 (MW)	30.000	30.000	27.768
PG6 (MW)	31.711	33.300	33.351
Time (sec)	89.7484	3.3319	8.03545
PL (MW)	10.762	11.200	10.970
Fuel Cost (\$/hour)	1111.24	1082.10	1081.3329
Emission (lb/hour)	540.295	539.90	539.1846

Table 15: Results of EED of IEEE 30 bus system for load demand of 350 MW.

Algorithm		NSGA-II	MOPSO	MODE-RDC
Generation Distance (GD)	Minimum	0.064384	0.1329	0.056721
	Maximum	0.162268	0.1329	0.391057
	Average	0.094781	0.1329	0.093724
	Standard deviation	0.025093	0.0000	0.056003
Spacing (S)	Minimum	0.474948	0.7443	0.403432
	Maximum	1.483643	0.7443	3.664206
	Average	0.789943	0.7443	0.741615
	Standard Deviation	0.255086	0.0000	0.609410
Diversity (A)	Minimum	0.807397	0.5516	0.509509
	Maximum	1.353364	0.5516	0.958338
	Average	1.095059	0.5516	0.531211
	Standard deviation	0.136457	0.0000	0.069968

Table 16: Performance of algorithms for IEEE 30 bus system at load demand of 350 MW.

Load (MW)	Algorithm	MODE-RDC Wins	MODE-RDC Losses	Detected differences
200	NSGA-II	14	11	-
	MOPSO	13	12	-
283.4	NSGA-II	13	12	-
	MOPSO	15	10	-
350	NSGA-II	13	12	-
	MOPSO	13	12	-

Table 17: Result of sign test on MODE-RDC algorithm on IEEE 30 bus system with GD metric as winning parameter.

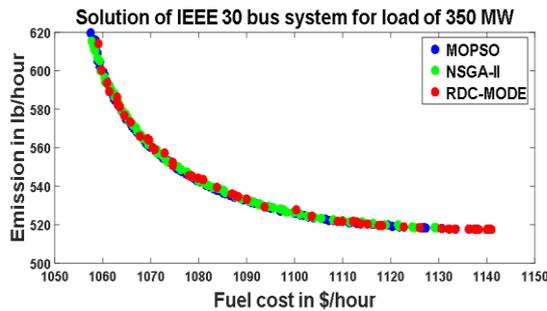


Figure 1: Solution of IEEE 30 bus system for load demand of 350 MW.

Load (MW)	Algorithm	MODE-RDC Wins	MODE-RDC Losses	Detected differences
200	NSGA-II	16	9	-
	MOPSO	13	12	-
283.4	NSGA-II	14	11	-
	MOPSO	16	9	-
350	NSGA-II	13	12	-
	MOPSO	13	12	-

Table 18: Result of sign test on MODE-RDC algorithm for IEEE 30 bus system with S metric as winning parameter.

6.2.4 IEEE-30 bus system: summary of results

The summary of results for this test case with the three load demands by applying all the three algorithms is presented in Tables 11, 13 and 15. It shows that the fuel cost obtained using the proposed algorithm provides improved performance as compared to other two algorithms. The transmission loss involved with the generation schedule thus arrived is also lower. The quality of solutions arrived using the algorithms is further estimated from pair wise sign test [21] on 25 runs of the algorithms. The results are presented in Tables 17, 18 and 19. Based on the number of wins and losses it is observed from Tables 17, 18 and 19 that the solutions obtained by applying the proposed algorithm yield lower average values in terms of all the three performance metrics. So, these solutions can be considered to be better than those from the other two algorithms. Also, the proposed MODE-RDC algorithm does not perform very well in terms of GD and S metric as in case of IEEE 30 bus system for load demand of 350 MW as depicted in Tables 17 and 18. This is clear in these tables as it does not have a significant detected difference that needs at least 17 wins out of 25 runs. This is due to the reduction in the number of non-dominated solutions in the successive iterations in the proposed algorithm.

Here, it can be pointed out that in most cases the average value of S metric has increased with rise in load demand for all the three algorithms this can be verified from Tables 2, 4 and 6 for test case I and Tables 12, 14 and 16 for test case II. This is due to the fact that when the load demand on the system rises, the size of the feasible space decreases due to the generator limits. The situation is further limited by the power balance constraint as the transmission losses increase with

Load (MW)	Algorithm	MODE-RDC Wins	MODE-RDC Losses	Detected differences
200	NSGA-II	15	10	0.05
	MOPSO	13	12	-
283.4	NSGA-II	14	11	0.05
	MOPSO	13	12	-
350	NSGA-II	23	2	0.05
	MOPSO	12	13	-

Table 19: Result of sign test on MODE-RDC algorithm for IEEE 30 bus system with Δ metric as winning parameter.

Gen no	1	2	3	4	5
Max MW	250	140	100	120	45
Min MW	10	20	15	10	10
γ	0.0126	0.02	0.027	0.0291	0.029
β	-0.9	-0.1	-0.01	-0.005	-0.004
α	22.983	25.313	25.505	24.9	24.7
a	0.00375	0.0175	0.0625	0.00834	0.025
b	2.0	1.75	1.0	3.25	3.0
c	0	0	0	0	0

Table 20: IEEE 14 bus system cost and emission coefficients.

Gen no	1	2	3	4	5	6
Max MW	200	80	50	35	30	40
Min MW	50	20	15	10	10	12
γ	0.0126	0.02	0.027	0.0291	0.029	0.0271
β	-0.9	-0.1	-0.01	-0.005	-	-
α	22.983	25.313	25.505	24.9	24.7	25.3
a	0.00375	0.0175	0.0625	0.00834	0.025	0.025
b	2.0	1.7	1.0	3.25	3.0	3.0
c	0	0	0	0	0	0

Table 21: IEEE 30 bus system cost and emission coefficients.

increase in power generation. Thus, the feasible solutions fall apart causing increase in the spacing parameter.

7 Conclusion

A set of three multi-objective optimization algorithms have been applied to solve the EED problem for two test cases on three different load demands. The performance of the proposed MODE-RDC algorithm along with other two is assessed by considering three different performance metrics. The performances of these algorithms have been critically analyzed. The Pareto optimal fronts obtained by all the three algorithms incorporating the proposed recursive distributed constraint handling technique have sufficient diversity by exploiting the entire available range of search space. In particular, the Pareto front obtained by the multi-objective differential evolution with the recursive distributed constraint handling (MODE-RDC) approach has a better diversity in most cases. The spacing between the Pareto solutions has found to be increased with rise in the load demand on the system for all the three

algorithms. Moreover, the time requirement to achieve the Pareto front by applying the proposed recursive distributed constraint handling based technique is satisfactory.

Further research on this topic may include the inclusion of different evolutionary local search mechanisms into the approaches. It is expected to obtain lower computational speed and exploitation of the multi-dimensional search space. There is a need for further investigation to explore the strengths and weaknesses of the proposed algorithm, so that it can be applied to other multi-objective problems in power systems, such as management of voltage profiles, reactive power compensation etc. The performance of the proposed algorithm can also be investigated by considering other real world constraints like ramp rate limits, power loss etc.

Appendix

The standard test cases taken for the solution are IEEE 14 bus and IEEE 30 bus power systems. The parameters of the test cases have been adopted from standard sources. The cost and emission coefficients used for solution of the problem are shown in tables 20 and 21 below.

The values of B coefficients used for the IEEE 14 bus test case are

$$B = \begin{bmatrix} 0.0208 & 0.0090 & -0.0021 & 0.0024 & 0.0006 \\ 0.0090 & 0.0168 & -0.0028 & 0.0035 & 0.0000 \\ -0.0021 & -0.0028 & 0.0207 & -0.0152 & -0.0179 \\ 0.0024 & 0.0035 & -0.0152 & 0.0763 & -0.0103 \\ 0.0006 & 0.0000 & -0.0179 & -0.0103 & 0.0476 \end{bmatrix}$$

$$B0 = [-0.0001 \quad 0.0023 \quad -0.0012 \quad 0.0027 \quad 0.0011]$$

$$B00 = 3.1826 \times 10^{-4}$$

The values of B coefficients used for the IEEE 30 bus test case are

$$B = \begin{bmatrix} 0.0218 & 0.0103 & 0.0010 & -0.0025 & 0.0007 & 0.0033 \\ 0.0103 & 0.0233 & 0.0001 & -0.0043 & 0.0009 & 0.0032 \\ 0.0010 & 0.0001 & 0.0525 & -0.0380 & -0.0111 & -0.0066 \\ -0.0025 & -0.0043 & -0.0380 & -0.1011 & 0.0132 & 0.0045 \\ 0.0007 & 0.0009 & -0.0111 & 0.0132 & 0.0163 & -0.0001 \\ -0.0033 & 0.0032 & -0.0066 & 0.0045 & -0.0001 & 0.0270 \end{bmatrix}$$

$$B0 = [-0.0002 \quad 0.0029 \quad -0.0033 \quad 0.0035 \quad 0.00016 \quad 0.0048]$$

$$B00 = 0.0025$$

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