

# An Improved Lag-Time Compensation Technique in Distributed Networked Control System Based on Smith Predictor

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*The geographically distributed feedback control loops connected via communication network elucidate the core of networked control system (NCS), wherein different users spread all over the world can regulate, direct and command the components of control system located at distant location. The proficiency of NCS provides sceptre to its user and multifaceted assignments are successfully endowed through it. The ascendancy of NCS is lowered through inconspicuous delays which destabilize the system. The induction of delays in the network lead to the proscription of packet delivery, bandwidth utilization and stable system response. In this manuscript Smith predictor is modified using Markov approach and Kalman estimation algorithm. The scheme has been implemented by using Matlab/ Simulink software for delay compensation. Performance analysis shows the robustness of modified Smith-Predictor controller in comparison to classical Smith predictor controller and proportional-integral-derivative based controllers.*

*Povzetek: V prispevku je predstavljena nova tehnika za uravnavanje časovnih zaostankov v porazdeljenih nadzornih mrežnih sistemih.*

## 1 Introduction

Rapid progress in communication technology has changed the perspectives of automation and control methodologies. Over the past few years; convergence of communication network and control system gave rise to the networked control system (NCS) as a novel approach of controlling the process or plants from a remote location. In NCS, to achieve the desired output, feedback control loops are spatially shared among the distributed actuators and sensors over the communication network [1]. In contrast to traditional point-to-point cable communication among various parts in a control system; the networked control system acquires less space, reduction in cabling complexity and power requirement that will lower the total installation and maintenance cost and hence, in turn will improve the reachability [2]. All these advantages have made the NCS popular among a wide range of applications including mobile robotics, traffic monitoring and control, aviation and satellite, defense and health care

sector, etc. There are certain challenging issues such as time-variations in transmission, problem in network schedulability, network-induced delays, packet loss and bandwidth utilization etc., [3]. These days research community is taking keen interest towards these important problems related to NCS.

In networked control system, the randomness in network-induced delay is most noteworthy phenomenon that may occurs normally due to the limited channel bandwidth, network congestion, multipath transmissions or may be caused by a node waiting for the acknowledgement to transmit data over the channel. To maintain the high packing efficiency of data for multi-packet transmission is also a challenging issue as all the scattered information is required to be packed [4]. During a transaction, due to the randomness, transmitted packets over the network are likely to be received in chaos that may lead to the packet dropout. In general, the data packet

dropout means delay in receiving the data at the receiver node tends to infinite is mainly caused due to existence of

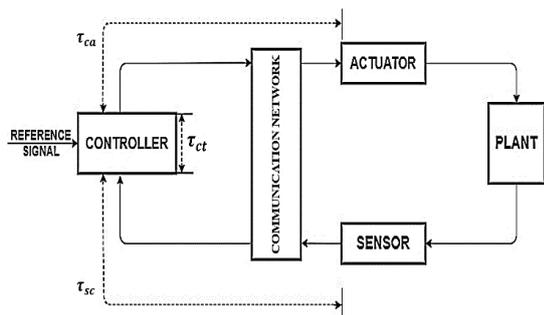


Figure 1: Major delays occurred in an NCS.

randomness in network-induced delays [5, 6]. These network-induced delay affects the output response of the NCS which deprave the dynamic performance and also deteriorate the stabilized-control efficiency of the networked control system [7, 8]. Conventional control theory also finds it difficult to achieve at the solution of delay induced dynamical system, therefore, it is necessary to highlight the modeling of random network-induced delay while designing the NCS. Solution of the network-induced random delay problem was sought by designing a networked predictive-controller [9]. Later on, networked predictive controller was advanced to facilitate the issues of constant and random network delays both in the forward and feedback channel [10, 11].

For NCS, a better system performance pretty much depends upon the timely reception of control signal by actuator and feedback signal truthfully measured by the sensor and its transference to the controller with infinitesimally small delay through communication network. Shown as in the Fig. 1, two types of network-induced delays are associated with the networked control system.

The feedback delay or sensor-to-controller delay can be tracked in feedback channel between sensor and controller whereas, the feedforward delay or controller-to-actuator delay can be traced between controller and actuator through the network. Figure 1 shows that controller and the plant are separated by a communication network which signifies the geographical reachability of the controlled operation but it also arises aforementioned delays.

In its intelligibly form the NCS can be represented in its state space model described as:

$$x(k + 1) = Ax(k) + Bu(k - \tau_{total}) \tag{1}$$

$$y(k) = Cx(k)$$

where,  $x \in R^n$  signifies system state vector,  $u \in R^m$  represents the control input vector to the system, the matrices like A and B are system matrix and input matrix with their suitable dimensions and  $\tau_{total}$  represents the total delay in the networked control system that majorly comprises of delay observed by controller due to sensor (s-c delay), delay spotted by actuator while transmitting

packet from controller (c-a delay) and computational delay.

Hence, in NCS the prime concern is based upon the three delays as shown in Figure 1 are related as:

$$\tau_{total} = \tau_{sc} + \tau_{ca} + \tau_{ct} \tag{2}$$

the three types of delay mentioned in the equation (2), are sensor to controller delay  $\tau_{sc}$ , controller to actuator delay  $\tau_{ca}$  and computational delay occurred due to the time taken by the controller to generate control signal for the actuator  $\tau_{ct}$  in a networked control system.

To focus upon the networked induced delays the effect of computational delay  $\tau_{ct}$  is ignored in this literature, the networked persuaded delays can be curtailed to reduce the total delay of the system. Most of the researchers have implemented proportional-integral-derivative based Smith predictor controller to minimize the delay but did not mentioned about the uncertainty in the delay and estimation of the model for prediction [12, 13]. The main issue lies with the uncertainty observed in the network-induced delay which causes instability that are difficult to judge. So, an estimation of the randomness of delay and accuracy in the estimation of state model of the system is introduced in this paper. For which, Markov approach and Kalman estimation is considered in the literature in the feedback channel to estimate feedback delay in a Smith predictor controller [14, 15]. The remaining part of the manuscript is elaborated as follows: Section 2, explain the necessity of smith predictor, its limitations and the design of smith predictor for networked control system based on Markov approach and Kalman estimation. In Section 3, the simulation results are presented and compared to evaluate the best suited controller to bring improvement in the performance of the networked control system, followed by conclusion in Section 4.

## 2 Development of Markov-Kalman based Smith predictor

In the design of a NCS, time delay has been considered an important performance constraint. The sluggishness observed in the system response due to PI control action is improved with the incorporation of derivative action [16, 17]. The robust performance for a wide range of operation fasten the Proportional-Integral-Derivative (PID) controllers for a variety of applications in the industry. Additional phase lag in the processes due to long

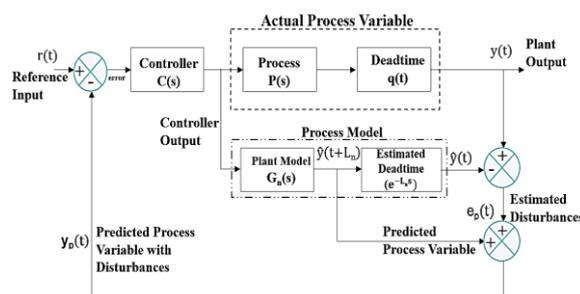


Figure 2: Classical Smith Predictor Model.



Since random time delay occurs across the network. The two types of delay include s-c and c-a called feedback and feedforward delays [26]. The feedback delays are more important as control inputs are function of feedback inputs. Delays lead to the packet dropout so it is important to cater them carefully so as to ensure the early prediction for the system state and input control signal [27]. The markov chain can be used to model the feedback in the state form and stabilization of the system can be obtained by optimizing the modeled state. Suppose  $\tau(t)$  represent the delay of the feedback channel being modeled by markov chain [28,29]. As each component of a chain every other component similarly, while designing state of delay using markov chain delay measured (observed) in the one cycle will affect the future delay measurement, or we can say that previous state of delay will affect the current delay. So, the modeling of homogeneous markov chain for  $\tau(t)$  can take values.

$$\bar{X}_2 = \{0,1,2,\dots,x_2\}$$

X denotes network switches between s-c,  $\alpha(t)$  denotes the state s and  $\alpha(t) \in [0,1]$

When X is in  $\alpha(t) = 0$ , depicts the successful reception of data packet and

$$\bar{y}(t) = y_p(t - \tau(t))$$

Whereas if X is in the state  $\alpha(t) = 1$  the packet is lost

$$\bar{y}(t) = y_p(t - 1)$$

The modelling of sensor-to-controller delay can be represented as,

$$\bar{y}(t) = (1 - \alpha(t))y(t - \alpha(t)) + \alpha(t)\bar{y}(t - 1) \tag{4}$$

where,

$$\alpha(t) = \begin{cases} 0, & \text{if packet received shows X is closed} \\ 1, & \text{if packet is lost thus the packet is lost} \end{cases}$$

Now, input to mode dependent output feedback controller presented as:

$$u(t) = K(\alpha(t), \tau(t))y(t) \tag{6}$$

Here,  $K(\alpha(t), \tau(t))$  is output feedback controller gain.

Suppose,  $s(t) = [s_p(t)^T \quad \bar{y}(t - 1)^T]^T$  is augmented state vector. For control vector (6) the closed loop system of (1) becomes,

$$s_a(t + 1) = A[s_p(t)^T \quad \bar{y}(t - 1)^T]^T + BK(\alpha(t), \tau(t))\bar{y}(t) \tag{7}$$

$$s_a(t + 1) = \bar{A}(\alpha(t))s(t) + \bar{B}(\alpha(t))Hs(t - \tau(t))$$

$$s(t) = \varphi(t)$$

$$t = -\tau_{\max}, -\tau_{\max} + 1, \dots, 0$$

Here,

$$\bar{A}(\alpha(t)) = \begin{bmatrix} A\alpha(t) & BK(\alpha(t), \tau(t)) \\ 0 & \alpha(t)I \end{bmatrix}$$

$$\bar{B}(\alpha(t)) = \begin{bmatrix} (1 - \alpha(t))BK(\alpha(t), \tau(t))C \\ (1 - \alpha(t))C \end{bmatrix}$$

$H = [I \quad 0]$ ,  $\tau_{\max} = \max(\tau(t))$  and  $\varphi(t)$  is initial condition of  $x(t)$ .

In the system (7),  $\{\alpha(t), t \in Z\}$  and  $\{\tau(t), t \in Z\}$  are two independent discrete time homogeneous markov chains

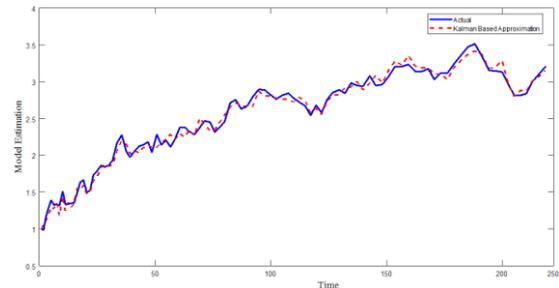


Figure 5: Model estimation of plant.

taking values in a finite set  $\bar{X} = \{0,1\}$  and  $\bar{X}_2 = \{0,1,2,\dots,x_2\}$  with transition probabilities:

$$P_r \{ \alpha(t + 1) = j \mid \alpha(t) = i \} = \Pi_{ij} \text{ from } i \text{ to } j.$$

$$\Pi_i = P_r(\Pi_0 = i)$$

$$P_r \{ \tau(t + 1) = n \mid \tau(t) = m \} = \lambda_{mn} \text{ from } m \text{ to } n.$$

where,  $\Pi_{ij} \geq 0$  and  $\lambda_{mn} \geq 0$  for all  $i, j \in Z_1, Z_2$

$$\sum_{j=0}^1 \Pi_{ij} = 1 \quad \text{and} \quad \sum_{n=0}^{x_2} \lambda_{mn} = 1$$

For  $\alpha(t) = i$ ,  $i \in \bar{X}_1$  and  $\alpha(t)$  in mode  $i=0$  and  $i=1$  the  $\alpha(t)$  in (7) take value  $\alpha(t) = 0$  and  $\alpha(t) = 1$  respectively.

$\bar{A}(\alpha(t))$  and  $\bar{B}(\alpha(t))$  are known constant matrices of appropriate dimensions.

The closed loop in equation (7) is a markov jump linear system with two markov chains that describe the behavior of the system for s-c time delays and packet dropouts respectively. This enables to analyze and synthesize such NCS by applying markov jump linear system and help us to estimate the modified state space model of the plant [30,31]. The Markov approach estimates the uncertain feedback delay and compares for estimated disturbance  $e_p(t)$ , which modify the disturbance variables for the predicted process.

### 3 Results and discussion

To illustrate the effectiveness of the proposed modified smith predictor it is compared with different controllers such as PI, PD, PID and Smith predictor. A comparison is drawn in Table 2. The modified smith predictor gives 34.16% improvement in settling time as compared to conventional Smith predictor, which shows that modified Smith predictor is an effective deadtime compensator for a stable process with long time-delays. The delay induced is modeled using Markov approach as shown in Figure 6, representing the transfer function of the plant model is

$$P(s) = \frac{127}{s^3 + 15s^2 + 83s + 101.3} \tag{8}$$

The stability problem can be solved by decreasing the controller gain. However, in this case the response obtained for smith predictor is very sluggish about 519.024/ksec which is further improved by modified Smith predictor 71.337/psec, a faster slew rate improves the bandwidth of the system and hence reduce the time delay and probability of packet dropout. The model estimation for the prediction of ideal state of the plant is

performed through Kalman estimation algorithm as shown in Figure 5.

PID controllers are the workforce of the industry but with the high demand of precision they are becoming sluggish the response of the PI, PD and PID can be observed from the Figure 7(a). The slew rate of the simulated controllers for networked control system can be compared from Table 2. Where lowest slew rate is

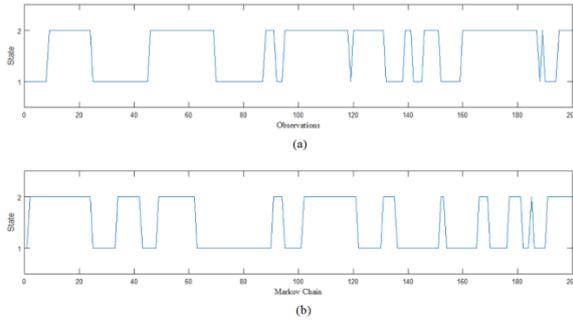


Figure 7: (a) Markov model-based observation (b) Sequence of Markov Chain.

Parameters	Type of Controllers		
	PID	Smith Predictor	Proposed Modified Smith Predictor
Rise Time (units of time)	0.572 sec	0.0015 sec	0.00012 sec
Slew Rate (per units of time)	1.398 /sec	519.024 /ksec	71.337 /psec
Preshoot (in %)	0.521	0.505	0.505
Overshoot (in %)	3.646	0.501	0.505
Undershoot (in %)	1.996	1.997	-0.505
Settling Time (in Sec)	0.39 sec	0.48 sec	0.316 sec

Table 2: Comparison of performance parameters of proposed modified Smith predictor controller with conventional controllers.

provided by PI controllers and higher slew rates in modified Smith predictor structure can be observed which offers a robust improvement in performance of closed loop over traditional controllers for stable processes.

In our design we have used values,  $P = 2.0$ ,  $I = 3.4$  and  $D = 0.1$  for a continuous-time PID controller to design the modified Smith predictor for networked control system with state space model of stepper motor represented as:

$$A = \begin{bmatrix} -11 & -91 & -108.3 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}, B = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, C = [0 \ 0 \ 107] \text{ and } D = [0]$$

The NCS has broadly two types of applications, one is time sensitive i.e., time critical and second is time insensitive applications also termed as time non-critical applications.

## 4 Conclusion

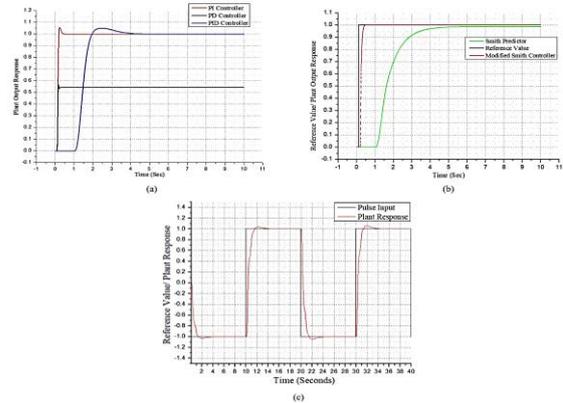


Figure 6: (a) Comparison of Plant Response using PI, PD and PID Controllers, (b) Comparative response of proposed modified predictive controller and conventional Smith predictor, (c) Response of proposed modified predictive controller to pulse input is evident from the Figure 7(b) that the modified Smith predictor have rise-time of  $1.2 \times 10^{-6}$  sec which is suitable for time sensitive applications such as medical and defense applications. From Figure 7(c) the impulse response of the modified Smith predictor can be observed with rise time of 0.78 sec and overshoot of 1.9%.

In case of NCS, network-induced delays are found very critical because these delays severely affect the performance of system. In order of compensate these delays, this paper proposes a modified Smith predictor controller. Proposed predictive controller adopts the Markov modeling for estimation of random delays and Kalman predictive approach is implemented to estimate the plant model of the Smith predictor model. Therefore, based upon these modifications proposed predictive controller is able to compensate effectively the delays with uncertainty. In this paper simulations with help of Matlab/ Simulink have been performed for various delay compensation schemes. Results ensure that the proposed modified Smith predictive controller scheme have a noteworthy improvement over Smith Predictor (without Markov) and other conventional controllers in terms of rise-time, slew rate, overshoot and settling time. Hence it can be précised that proposed modified predictor is appropriate for time critical applications where delay with randomness influences the performance of networked control system.

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