## **Surrogate Estimators For Collaborative Decision**

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We deal here with job scheduling under the assumption that performing a job requires the production of encapsulated renewable and non-renewable resources. For the sake of understanding, we rely here on a case study related to energy production by a photo-voltaic platform. Handling it means synchronizing resource production and consumption in order to optimize both production costs and some scheduling criterion, and induce the setting of a complex bi-level model. Moreover, this applicative context makes appear that job scheduling and resource production most often depend on distinct players, provided with their own agenda and access to information. Adopting here the point of view of one specific player, namely the job scheduler, leads us to set a model that shortcuts the production level with the help of surrogate estimators. Those estimators involve flexible pricing mechanisms and machine learning devices. According to this, we first perform a structural analysis of our model, before designing and testing several algorithms that implement this surrogate component based approach.

Povzetek: Poročilo obravnava problem načrtovanja nalog z uporabo obnovljivih in neobnovljivih virov energije, kjer se osredotoča na sinhronizacijo proizvodnje in porabe energije. Predlaga uporabo nadomestnih ocen za obvladovanje kompleksnih dvo-nivojskih odločitev v sodelovalnih okoljih, pri čemer vključuje tudi strojno učenje za optimizacijo stroškov.

## **1** Introduction

The notion of multi-level decisional model (see [16], [18]) most often derives from contexts involving several players, independent from each other or tied together by some hierarchical or collaborative link, who share the decision with respect to some system. Solving such a model aims either at providing a best scenario if all the players operate under a common authority (centralized paradigm), or (collaborative paradigm) at helping them into the search for a compromise.

Most contributions address multi-level models according to the centralized paradigm, while assuming the existence of a unique decider provided with full information. Handling a model set this way is a difficult task (see [10], [11]). It usually involves complex decision sub-models of very different types. Standard approaches rely on decomposition schemes, hierarchical (Benders decomposition, Stackelberg Equilibrium,...) or horizontal (Lagrangean relaxation) (see [2], [26]). In both cases a major difficulty derives from the sensitivity issue, which means the way one may retrieve information from the different levels in order to make them interact. In case the decision problem involves temporal constraints about jobs to be processed, another difficulty comes from resulting synchronization constraints (see [9]), which require the different players to meet in order to exchange resources or informations.

Yet in practice, it may be utopian, for both technical and economical reasons, to assume that all players will agree on a common agenda and on the share of information. *Game Theory*, mainly *Cooperative Game* (see [7], [8], [21],[33]), provides us with a useful tool for the anticipation of the behavior of the players and for the distribution of the costs among them. But it does not help a specific player in making its own decision. So, when the focus is on such a specific player, one must find a way to bypass the levels related to the other players and replace, under incomplete information, the criteria and costs related to those players by surrogate estimators.

Present contribution reflects this concern. If we refer to the Frascati Manual of the European Commission, it refers to Section I.2 (Informatics and Information Sciences) while involving developments related to Combinatorial Optimization and Operations Research. It refers to fundamental research in the sense that collaborative decision and complex multi-level models are generic issues, and it has also to see with Applied Research since, in order to make things easier to understand, we start from an applicative context. This context is related to researches conducted about intelligent vehicles inside the IMOBS3 (*Innovative Mobility Services, Systems and Structures*) Labex in Clermont-Ferrand, and to a partnership between LIMOS Laboratory and the national PGMO (*Gaspard Monge for Optimization*) program promoted by power company EDF (*Electricity De France*). It involves the joint management of energy by a local photovoltaic (PV-Plant) platform and by a consortium of users (industrial players, services providers, ...) relying on this energy in order to perform jobs according to their own purposes. The fact is that market deregulation and emergent technologies currently induce the rise of local renewable energy producers (factories, farms, householders, ...) who simultaneously remain consumers. Those new players make *self-consumption* become an issue (see [5], [22], [30], [36], [44]) whose key operational feature is the need for synchronization between time-dependent resource production and its consumption (see [12], [14], [23], [25]).

So we consider here on one side, a production manager who runs a PV-Plant (Photovoltaic Plant), that not only produces energy and distributes it among end-users (jobs) but also buys and sells energy on the market. On the other side, one or several job schedulers are in charge of performing specific jobs. Both meet in order to perform recharging transactions: in order to avoid jobs to waste time while waiting for recharge, the PV-Plant relies on a set of batteries and implement a *swapping* policy (see [4], [40], [41]), so that the job schedulers only need to switch from a battery to another one. We suppose that this plug out/in operation is instantaneous. Limited storage and recharge capacities impose both players to carefully synchronize the time-dependent energy production and its consumption. This requirement makes resulting bi-level decision problem complex, even under the centralized paradigm. Many searchers recently showed interest into the decisional problems raised by the management of renewable energy. They most often focused either on production scheduling (see [1], [13], [15]) or on the issues related to consumption (see [3], [17], [19], [27], [31]). But very few dealt with the interaction between both (see [5], [6], [23], [34], [36], [40]) and they most often did it while adopting the point of view of a unique decider provided with full information. Our goal is to study here this interaction and the way players collaborate under incomplete information (see [12], [29], [34], [35]), in order to derive heuristic algorithms reflecting the point of view and the knowledge of a specific player. Though part of the difficulty of our specific application is due to uncertainty, we suppose, for the sake of simplicity, that our system behaves in a deterministic way.

Starting from this applicative context, we set a bi-level **PVSync** model. This model is a centralized macroscopic model, which relies on simplifications with respect to the behaviors of respectively the batteries and the PV-Plant (linearization of the charge and discharge processes for the batteries (see [37], [38], [39]), deterministic power prediction for the PV-Plant (see [44]). Those simplifications are justified not only by our wish to get a tractable model, but also by the fact that we intend adopting the point of view of the job scheduler and designing heuristic

algorithms that reflect this point of view. We notice that this **PVSync** model may be viewed as a new variant of the well-known **RCPSP**: *Resource Project Scheduling Problem*(see [32], [24]). **RCPSP** is about scheduling jobs under temporal and resource constraints, and our model introduces non-renewable resources (energy) encapsulated into renewable ones (the batteries).

We first study PVSync according to the centralized paradigm. We cast it into the MILP: Mixed Integer Linear Programming framework, and analyze the structure of its main components. Our main purpose being the design of heuristics reflecting the point of view of the job scheduler, we introduce a *projection* mechanism that projects the constraints related to the batteries, that the job scheduler does not control, into a surrogate Idle Battery constraint that he may easily handle. Next, we address the collaborative issue. We start doing it while supposing that the production manager acts as a mediator, and cast our problem into the Cooperative Game framework. We keep on while adopting the point of view of the job scheduler, who implicitly endorses the role of the master of the game. Our goal becomes the design of *job scheduler* oriented heuristic algorithms SurrPVCost that handle PVSync according to this restricted point of view, while short-cutting the part of the process involving the PV-Plant. We use a surrogate formulation of the costs together with surrogate constraints that aims at making the hidden production level remain feasible. The surrogate constraints are the Idle Battery projected constraints that we just mentioned above, augmented with additional constraints. As for the surrogate formulation of the costs, we try two approaches: the first one is based upon a pricing mechanism; the second involves machine learning and convolutional neural networks (see [28], [43]). Both approaches are well-fitted to the management of the non-deterministic case.

So the paper is organized as follows. In Section 2, we introduce the **PVSync** problem. We set it according to the centralized MILP (Mixed Integer Linear Programming) framework (Section 2.2), and discuss different formulations (Section 2.3). In order to help the reader in identify the scope of the paper we fix the limitations of this research in Section 2.4.In Section 3, we analyze the structure of the main components of this model and the properties of the *Idle Battery* constraint. We start discussing in Section 4 the cooperative issue and first cast in Section 4.1 our problem into the Cooperative Game framework. Next we introduce in Section 4.2 a generic collaborative algorithmic scheme for the handling of PVSync while using surrogate estimators. We describe in Section 4.3.1 the surrogate constraints that we derive from the projection scheme of Section 3, and propose in sections 4.3.2 and 4.3.3 2 estimators of the production costs: the first one relies on a parametric pricing mechanism while the second one involves a convolutional neural network. We describe in Section 4.4 the way those estimators may

be used in order to drive a *job scheduler* oriented heuristic algorithm *SurrPVCost*, and devote Section 5 to numerical experiments.

## 2 The PVSync problem

This section is devoted to the description of our case study, related to energy management, which will be the starting point for coming developments. As told in the introduction, this case study derives from a partnership between the LIMOS Laboratory and the national PGMO (Gaspard Monge for Optimization) promoted by power producer EDF. It provides us with a medium for the implementation and the tests of algorithmic proposals related to a more fundamental issue, namely the management of complex multi-level decision models in both centralized and collaborative contexts. According to this, our main contribution will be about the way we may endorse the point of view of a given specific player, set a model reflecting its agenda and access to information, that consequently reduces the behavior of the other players to what we call surrogate constraints and criteria, and accordingly design heuristic algorithms.

While setting a model for this case study, we shall notice that it extends one of the most fundamental scheduling problem, the **RCPSP**: *Resource Constrained Scheduling Problem*.

The Job Scheduler Side: We consider a set of *jobs*  $J = \{1, ..., J\}$  to be performed exactly once within a time horizon [0, N] divided into unit length periods. We denote by *i* the period [i - 1, i]. Any job *j* requires  $t_j$  periods and is constrained by a time window  $\{Min_j, ..., Max_j\}$ : *j* must start no sooner than period  $Min_j$  and end at period no later than  $Max_j$ . Some pair of jobs  $(j_1, j_2)$  are tied together by some precedence relations  $j_1 << j_2$  whose meaning is that  $j_1$  must be finished when  $j_2$  starts. We do not allow *Preemption*: Once a job starts, it cannot be interrupted.

The Resources : Every job j requires some amount of (electric) energy  $e_j$ . This energy is stored inside a set  $\mathbf{K} = \{1, ..., K\}$  of identical batteries, that are assigned to the jobs at the time when they start. Every job requires exactly one battery and a battery cannot be simultaneously assigned to several jobs. It comes that no more than Kjobs may be running at the same time. A battery must be periodically recharged in order to run as many jobs as possible, and *recharge* takes place when the battery is *idle* and does not run any job. The *storage* capacity of a battery is denoted by C: The amount of energy stored inside a battery cannot exceed C. The *recharge* capacity of a battery is denoted by  $C^R$ : The amount of energy which may be loaded into a battery during 1 period cannot exceed  $C^R$ . The initial load of battery  $k \in \{1, \ldots, K\}$  is denoted by  $H_k^{Init}$ . For technical reasons, assigning a battery to a job j takes place at the junction between 2 periods, that means at some time i, i = 0, ..., N - 1. Such a *swapping* transaction is instantaneous. The battery remains *active* during the time when j is running, and cannot be recharged during this time. We introduce the following notations:

$$- \hat{e} = \sum_{j} e_{j}; \hat{t} = \sum_{j} t_{j}; E^{Mean} = \frac{\hat{e}}{\hat{t}}$$
$$- \text{ For any } j, e_{j}^{Mean} = \frac{e_{j}}{t_{i}}.$$

Remark 1: We proceed here in a way that is standard with respect to this kind of problems (see [3], [19], [27]) and that consists in simplifying the physics of both the batteries and the PV-Plant. We implicitly refer here to the same kind of Ion/Lithium batteries that may be embedded into electric vehicles, with storage capacities between 20 KWh and 100 KWh, and recharge capacities between 10 KW and 100 KW. However, we do as if that the charge and discharge processes of those batteries were linear, that may be considered as true as long as the current charge of the battery remains located inside some critical interval (see [37], [38]). This implicitly means that capacity C is not the real capacity of the battery, rather the size of the interval inside which the charge and discharge processes may considered as quasi-linear. Also, we do not allow here any choice choice between different recharge capacities involving distinct economic costs.

**The PV-Plant Side**: In order to implement a *selfconsumption* policy we rely on a *PV-Plant*, that means on a photovoltaic facility. This PV-Plant assigns the batteries to the jobs according to some swapping policy and produces its own energy that it distributes among the currently idle batteries or that it sells to the market. In case this selfproduced energy is not enough, the PV-Plant can also buy energy to the market. Energy stored inside the batteries can be neither transferred to another battery nor sold. We de-



Figure 1: Time dependent production rates and costs for the micro-plant

note by  $R_i$  the expected production of the PV-Plant at period i, by  $P_i$  the energy unit purchase price at period i, and by  $S_i$  the energy unit sale price. Of course we have, for any  $i, P_i \ge S_i$ . An example of cost and production rates is provided by Figure 1. We set, for any period i:

-  $P^{Mean}$  = mean value  $P_i, i = 1, \ldots, N$ ;

- 
$$S^{Mean}$$
 = mean value  $S_i, i = 1, ..., N$ ;  
-  $R^{Mean}$  = mean value  $R_i, i = 1, ..., N$ 

Figure 2 describes the way the PV-Plant and the jobs interact in the case when the jobs are tours performed by electric vehicles, that start and end into the PV-Plant and make the vehicles visit a set of customers. It shows the swapping policy that makes some *active* batteries be embedded into the vehicles, while the other *idle* batteries remain available for recharge.

**Remark 1-Bis**: We bypass the physics of the PV-Plant (see [39], [44]) and consider its behavior as deterministic, following the way standard software like PVLib Matlab ([44]) proceed.



Figure 2: PV-Plant, batteries and vehicle routing jobs

Then we may set the **PVSync** problem:

**PVSync**: {Simultaneously schedule the jobs and the PV-Plant, in such a way that:

- Every job j is run once without any interruption (*Non-Preemption*) within its time window. Precedence constraints  $j_1 \ll j_2$  are satisfied. (C1)
- Every time a job j is performed, it is provided with a battery k(j) loaded with at least  $e_j$  energy. (C2)
- The global energy load of the batteries at the end of period N must be at least equal to  $\sum_k H_k^{Init}$ . (C3)
- Some hybrid cost α.SchCost+PVCost is minimized. PVCost is the self-consumption cost, equal to the difference between the energy purchase costs and the profits derived from the sales. Scheduling cost SchCost is the sum of the completion times of the jobs.}

**Remark 2: PVSync and the RCPSP problem**: The **PVSync** problem may be viewed as new variant of the

well-known **RCPSP**: *Resource Constrained Scheduling Problem* (see [32], [24] for standard RCPSP), that is itself an extension of the *Multi-Processor Scheduling* problem. Jobs depend here on *encapsulated* resources, which are renewable batteries and non-renewable energy embedded into the batteries. The first ones act as *containers* for the second ones. Setting this extension in a formal way would imply introducing a lot of notations, without any fundamental impact on the methods. So, instead of doing it, we keep on with the **PVSync** setting and terminology, while referring to the batteries as renewable container resources and to the energy as non renewable content resource.

**Remark 3** : We may set **PVSync** as a bi-level model by distinguishing the respective roles of the job scheduler and the PV-Plant :

- **Bi-level Reformulation of PVSync**: {Schedule the jobs in such a way :
  - (C1) is satisfied.
  - An hybrid cost  $\alpha \cdot SchCost + PVCost$  is minimized, PVCost being the optimal value of the following **PVPlant** sub-problem :
    - **PV-Plant sub-problem** : {Schedule the sale, purchase and distributions operations, and assign the batteries to the jobs in such a way that (C2) is satisfied and that the difference between the energy purchase costs and the profits derived from the sales is minimal.}}

**Remark 4**: One might clearly make the PV-Plant side more complex, by broadening the scope of feasible sale, purchase and distribution operations, by getting closer to the physics of storage and recharge/discharge processes, by involving Heterogeneous batteries, with distinct storage and recharge capacities, and by allowing distinct recharge capacities, each recharge capacity involving its own specific costs.

Our Goal and Contribution : As a new bi-level extension of the RCPSP problem, the PVSync problem is interesting by itself. Yet, our purpose here is not the design of exact algorithms for this problem, rather the study of the way one might efficiently handle it if the PV-Plant processes become more complex (see Remark 4) or in the case of a collaborative context, that would impose us to focus on the job scheduler point of view and cope with restrictions on the information related to the behavior of the PV-Plant. This means that our main contribution here is the design of heuristic algorithms that tends to emulate the decentralized point of view of a specific player, namely the job scheduler, possibly provided with partial information. In order to achieve it, we first cast PVSync into the MILP framework (Section 2.2), in order to get an unambiguous setting and to provide ourselves with reference results, and discuss

some variants (Section 2.3). Next we perform some structural analysis (Section 3) with focus on the introduction of a mechanism that projects the constraints related to the batteries (that the job scheduler does not control) into surrogate Idle Battery constraints that he may easily handle. The introduction of this projection mechanism opens the way (Sections 4 and 5) to the design and test of job scheduler oriented heuristic algorithms SurrPVCost for the handling of **PVSync**, that reflect the incomplete point of view of the job scheduler. These algorithms rely on the management of surrogate constraints, (the Idle Battery constraints augmented with some additional constraints), and of surrogate objective functions, that express the approximation that the job scheduler may get of the part of the costs that it does not fully control. Though we stick here to our case study, this approach is generic and might be applied to other multilevel/multi-player decision problems.

### 2.1 An example

Let us suppose that  $J = \{A, B, C, D, E\}$ , with respective durations  $t_j = 2, 1, 2, 3, 1$  and energy requirements  $e_j = 5, 5, 4, 9, 4$ . Jobs A and B must be run between periods 3 and 5, job C between periods 5 and 8, job D between periods 2 and 7, and job E between periods 7 and 10. We are provided with 2 identical batteries  $k_1$  and  $k_2$ , with initial loads respectively equal to 7 and 6. We have: C = 12,  $C^R = 3$ . The time space is divided into 10 periods and time versus money coefficient  $\alpha$  is equal to 2. Production data come as in table 1:

Table 1: Prices and production coefficients

i	1	2	3	4	5	6	7	8	9	10
$P_i$	2	3	7	7	3	2	6	7	4	2
$S_i$	1	2	4	4	1	1	3	3	2	1
$R_i$	4	4	3	5	2	6	4	4	4	5

Then we get (Fig. 3) a feasible PVSync solution:

- Battery  $k_2$  consecutively runs jobs A and B between periods 3 and 5 and comes back to the PV-Plant at the end of period 5. It reloads until period 7, runs job E and comes back to the PV-Plant.
- Battery  $k_1$  runs job D at period 2 and comes back to the PV-Plant at the end of period 4. Then it reloads before running job C at period 8.



Figure 3: A feasible schedule of the jobs

For every period i, energy amounts respectively bought, sold and distributed to the batteries are given by table 2.

Table 2: Scheduling the production

					0	1				
i	1	2	3	4	5	6	7	8	9	10
Bought	1	0	0	0	1	0	0	0	0	1
Sold	0	1	3	5	0	0	1	4	2	0
<b>To</b> <i>k</i> <sub>1</sub>	2	*	*	*	3	3	*	*	3	*
<b>To</b> <i>k</i> <sub>2</sub>	3	3	*	*	*	3 *	*	2	3	*

### 2.2 A MILP model

The purpose of this section is to cast the **PVSync** problem into the MILP framework. This will provide us with a non ambiguous formal setting of this problem, that we will refer to all along the paper, as well as with reference results for numerical experiments. Notice that it would have been possible to choose another framework, like for instance the SAT framework (while using the library Google's CP-SAT, part of the OR-Tools Library) or the Constraint Programming framework (while relying on the IBM CPO software). But the fact is that the MILP framework is a kind of standard in Operations Research and Combinatorial Optimization, and is also widely used in the Industry, specifically in companies involved in Telecommunications, Transportation and Energy Production.

Since **PVSync** may be viewed as a **RCPSP** extension, we adapt the standard **RCPSP** MILP: *Mixed Integer Linear Program* formulation corresponding to the case when the time space is explicitly divided into unit-time periods. In such a case, **RCPSP\_MILP** usually relies on a  $\{0, 1\}$ -valued vector  $Z = (Z_{j,i}, i = 1, ..., N, j = 1, ..., J)$  which tells us at which period *i* a job *j* starts. In our case, we must also explicitly identify the batteries so that they may be assigned to the jobs. We link the jobs, the periods and the batteries through a  $\{0, 1\}$ -valued vector  $X = (X_{j,k,i}, j = 1, ..., J, k = 1, ..., K, i = 1, ..., N)$ :  $X_{j,k,i} = 1$  means that battery *k* is assigned to job *j*, starting at period *i*.

On the other side, we represent the production activity of the PV-Plant by 3 non negative rational vectors  $U = (U_i, i = 1, ..., N), V = (V_i, i = 1, ..., N),$  $Q = (Q_{k,i}, k = 1, ..., K, i = 1, ..., N)$ , with respective meanings:

- $U_i$  means the energy purchase at period i,
- $-V_i$  represents the energy sale at period *i*,
- $Q_{k,i}$  represents the energy distributed to battery k at period i.

We link the PV-Plant, the jobs and the batteries through a last variable  $W = (W_{k,i}, k = 1, ..., K, i = 0, ..., N) \ge 0$  with rational values:  $W_{k,i}$  represents the energy inside battery k at the end of period i ( $W_{k,0}$  means the initial load of battery k). Resulting model comes as follows:

### PVSync\_MILP Model: {Compute:

- {0, 1}-valued vector  $Z = (Z_{j,i}, i = 1, \dots, N, j = 1, \dots, J)$ :  $Z_{j,i} = 1$  means that job j starts at period i.
- {0, 1}-valued vector  $Y = (Y_{j,k}, k = 1, \dots, K, j = 1, \dots, J)$ :  $Y_{j,k} = 1$  means that battery k is assigned to job j.
- {0, 1}-valued vector  $T = (T_{k,i}, k = 1, \dots, K, i = 1, \dots, N)$ :  $T_{k,i} = 1$  means that battery k is active at period i.
- {0, 1}-valued vector  $X = (X_{j,k,i}, k = 1, \dots, K, j = 1, \dots, J, i = 1, \dots, N)$ :  $X_{j,k,i} = 1$  means that battery k is assigned to job j, starting at period i.
- $-U = (U_i, i = 1, ..., N) \ge 0$  with rational values:  $U_i$  means the energy purchase at period *i*.
- $-V = (V_i, i = 1, ..., N) \ge 0$ , rational:  $V_i$  means the energy sale at period *i*.
- $Q = (Q_{k,i}, i = 1, ..., N, k = 1, ..., K)$ , rational:  $Q_{k,i}$  means the energy distributed to battery k at period i.
- $W = (W_{k,i}, i = 0, ..., N, k = 1, ..., K) \ge 0$ , rational:  $W_{k,i}$  means the load of battery k at the end of period i.

Under the constraints:

- Minimize  $\sum_{i} (P_i . U_i - S_i . V_i) + \alpha . (\sum_{j,i} i . Z_{j,i}).$ (E1)

- For any 
$$i, j, Z_{j,i} = \sum_k X_{j,k,i}$$
. (E2)

- For any 
$$k, j, Y_{j,k} = \sum_i X_{j,k,i}$$
. (E3)

- For any battery k, period 
$$i_1$$
,  $T_{k,i_1} = \sum_{j,i=i_1-t_j+1,\dots,i_1} X_{j,k,i}$ . (E4)

- For any  $j, \sum_{k} Y_{j,k} = 1 = \sum_{i} Z_{j,i} = 1.$  (E5)
- For any j, any i s.t  $(i < Min_j)$  or  $(i > 1 + Max_j t_j), Z_{j,i} = 0.$  (E6)
- For any  $k, i, Q_{k,i} \le C^R (1 T_{k,i}).$  (E7)

$$- \text{ For any } i, k, W_{k,i} \le C.$$
(E8)

- For any  $k, W_{k,0} = H_{k,0}^{Init}$  and  $W_{k,N} \ge H_{k,0}^{Init}$ . (E9)
- For any  $i \ge 1, k, W_{k,i} = W_{k,i-1} + Q_{k,i} (\sum_j e_j \cdot X_{j,k,i}).$  (E10)

- For any 
$$i, U_i + R_i = V_i + (\sum_k Q_{k,i}).$$
 (E11)

 $\begin{array}{l} - \mbox{ For any } j_1, j_2 \mbox{ s.t. } j_1 << j_2, \sum_i i.Z_{j_1,i} + t_{j_1} \leq \\ \sum_i i.Z_{j_2}. \end{array} \tag{E12}$ 

**Proposition 1**: Solving **PVSync\_MILP** solves the **PVSync** problem.

**Proof**: One easily turns any feasible solution of **PVSync** into a feasible solution (Z, Y, T, X, U, V, W, Q) of **PVSync\_MILP** with same cost. Checking that every constraint (E1),..., (E12) is satisfied derives in a straightforward way from the meaning of those constraints: (E2)

means that if job j starts at period i, then there is exactly one battery assigned to j. (E3) means that if battery kis assigned to job j, then there exists a unique period isuch that j starts with battery k at period i. (E4) means that if battery k is active at period  $i_1$ , then there exists a unique job j which starts with battery k at i such that  $i \leq i_1 \leq i + t_i - 1$ . (E5) means that to any job j must be assigned exactly one battery and one starting period. (E6) means that any job j is run within its time window. (E7, E8) are capacity constraints: the load inside a battery at the end of a given period cannot exceed the storage capacity of the battery, and the amount of energy loaded into a battery during a given period cannot exceed the recharge capacity. (E9) expresses the initial and final requirements for the batteries. (E10, E11) are nothing more than balance equations, which distribute energy over the time between purchase, sale, storage and consumption by the jobs. (E12) means that if two jobs  $j_1, j_2$  are such that  $j_1$  precedes  $j_2$ , then the starting period for  $j_2$  must be larger than the ending period of  $j_1$ . Conversely, the key point is that (E5) assigns exactly 1 battery k and 1 starting period i to every job, and that variables  $X_{i,k,i}$  involved in (E2, E3, E4) allow us to characterize the periods when a battery is active or idle. This in turn enables us to control through (E7, E11) the amount of energy loaded into any battery at any period, as well as the Non-Preemption constraint. The rest of the proof comes in a straightforward way. End-Proof.

### 2.3 A short discussion: variants of the PVSync problem

In practice, production configurations may be more complex (see Remark 4), and we may be imposed to get closer to the physics of both the batteries and the PV-Plant. Let us mention here 3 possible variants, whose handling would provide us with a stronger motivation for the approaches that we are going to describe in Section 4:

**First Variant**: Batteries may be used in order to store energy and sell it later. According to this hypothesis, a battery k may receive energy at period i and sell it at period i' > i. The **PVSync\_MILP** model must be updated through the introduction of an additional vector  $V^S = (V_{k,i}^S, k = 1, ..., K, i = 1, ..., N)$ , meaning the amount of energy sold at any period i by battery k.

Second Variant: A fixed storage unit may be used either for later sale or battery feeding. According to this hypothesis, such a Buffer battery BUFF, with storage capacity  $C^{BUFF}$ , initial load  $H^{BUFF}$ , recharge capacity  $C^{ReBUFF}$ and discharge capacity  $C^{DeBUFF}$ , induces the introduction of new variables into the model:

- $Q_i^{BUFF}$  = energy sent from the PV-Plant to the *Buffer* battery at period *i*.
- $V_i^{BUFF}$  = energy sold by the *Buffer* battery at period *i*.

- $Q_{k,i}^{BUFF} =$ energy sent by the *Buffer* battery to battery k at period *i*.
- $W_i^{BUFF}$  = energy inside the *Buffer* battery at the end of period *i*.

**Third Variant**: *Periods units and time values do not coincide.* 

Actually, the structure of the time space for the PV-Plant may not coincide with the structure of the time space for the jobs. More precisely, a period means a time interval during which the PV-Plant is stable (no change neither in the production rates nor in the purchase/sale prices). In most cases, the duration of a period is given as an integral number p, while the duration of a job may take any integral value. In such a case, representing the schedule of the jobs with a vector  $Z = (Z_{j,i}, i = 1, ..., N, j = 1, ..., J)$  as in the previous section does not hold anymore and getting a **PVSync** MILP formulation requires the introduction of flow vectors representing the way the jobs exchange the resources.

### 2.4 Limitations of the research

The present paper involves a wide range of concepts and software tools. To better delineate the scope of the paper and remove any ambiguity, we will summarize its limitations here. This will help the reader distinguish between concepts mentioned as potential future research topics and methods used as tools, from the issues that are central to the paper.

- The RCPSP is not central: We mention in the introduction and in previous section 2.2 that PVSync may be viewed as an extension or a variant of the standard **RCPSP** problem. This extension is novel in that it links renewable and non-renewable resources through an encapsulation relation (the renewable batteries are containers for the non-renewable energy). In the future, it may be interesting to further study RCPSP models linking renewable and non-renewable resources and to design new exact algorithms or adapt existing ones. However, this is not the purpose of this paper, which is in no way focused on the RCPSP. We do not cast PVSync into the generic RCPSP framework involving jobs and resources, nor do we focus on designing exact algorithms for handling it (typically, contributions about RCPSP presuppose a centralized context and emphasize the design of fast-running exact algorithms [24]).
- MILP models and solvers are tools, not the focus: At the beginning of former section 2.2, we provide a MILP formulation of PVSync. The main purpose of this MILP model is to establish an unambiguous formulation of the PVSync problem and to generate benchmark results that can help evaluate heuristic algorithms designed from the restricted perspective of a

specific player. We use the MILP framework primarily because we are familiar with the CPLEX Library. Consequently, our focus is not on designing sophisticated MILP settings for **PVSync** that involve valid cuts, facets, or specific decomposition schemes to facilitate the computation of exact solutions. In realistic contexts, the complexity of the production level (the PV-Plant) and the incompleteness of the information available to a target player would render such settings impractical. Instead, our goal is to design heuristic algorithms that are adapted to such complex contexts.

- The same applies to Machine Learning: Sections 4 and 5 of the paper will involve neural networks used to provide the job scheduler with an approximation of the behavior of its production partner. Since the behavior of this PV-Plant player is related to solving a production planning problem, we use convolutional neural networks (CNNs) to handle instances of this planning problem with varying sizes while limiting the number of synaptic coefficients. However, Machine Learning will not be our primary focus: We shall rely on standard, ready-to-use open software (Keras TensorFlow) that we apply to a CNN with a fairly intuitive structure, and we train this CNN using versions of the stochastic gradient algorithm implemented within this software. The accuracy of the neural network is not the critical factor here; rather, it is its ability to guide our heuristic scheduling algorithms toward satisfactory solutions.
- PV physics and technologies are only a hypothesis: Our paper addresses a decision problem from the perspective of a specific target player who bypasses some levels of the complex underlying system by using surrogate estimators. When referring to the physics behind this system, related to batteries and charge/discharge processes, we remain at a macroscopic level, and our decision models require significant simplifications. As explained in both the introduction and at the beginning of this section, these simplifications involve assuming that the recharge and discharge processes are linear and that the behavior of the PV-Plant is deterministic, which is generally accurate as long as the battery load remains within a safe interval. Therefore, we do not concern ourselves with the full infrastructure of the PV-platform (such as inverters and trackers) or what occurs at the microscopic level. In other words, our contribution is not about photovoltaic production technology, nor is it about the physics and electronics involved in the production and storage of this renewable energy.

## **3** Structural analysis

We analyze in this section the structure of **PVSync** and its complexity, while adopting the standard centralized point of view (one decider, provided with all information). We describe the projection mechanism (*Idle Battery* constraints) that will allow us to bypass the battery level. We first introduce the following notations:

- For any subset A of the job set J, we denote by **PVSync**(A) the restriction of **PVSync** to the jobs of A, and by PVSync(A) its value.
- For any schedule vector Z we denote by **Restrict**-**PVSync**(Z) the problem which derives from **PVSync** by fixing Z, and by RestrictPVSync(Z) its value.
- For any schedule vector Z and any period i, we denote by n(Z, i) the number of jobs which are active at period i according to Z, and by L(Z, i) = K n(Z, i) the number of batteries which are idle at period i, that means which are available for recharge.
- Given a schedule vector Z and a job j, we denote by Start(Z, j) the starting period of j according to Z.

# 3.1 The different levels of PVSync and their complexity

**PV-Sync** is a multi-level problem. We may distinguish a scheduling level (variables Z), a battery level (variables Y) and a production one (variables U, V, Q). This last one is nothing but a linear program with rational variables.

### The Scheduling Level

Restricting **PVSync** to its scheduling level means shortcutting the activity of the PV-plant, and only considering the jobs, provided with durations, time windows and precedence constraints, together with K identical batteries which lose their container status and behave as machines in the standard scheduling sense. In the case of variant 3 of former section 2 this restriction of **PVSync** to its scheduling level would contain the multi-machine scheduling problem, and so would be NP-Hard (see [20], [42]). Since our time space is explicitly divided into periods, we must be more careful. Let us consider the following setting **PVSync**:

### **PVSync-Sched**

- Inputs:
  - The period set  $\{1, \ldots, N\}$
  - The battery set  $\mathbf{K} = \{1, \dots, K\}$
  - The job set  $\mathbf{J} = \{1, \ldots, J\}$ : A job j requires  $t_j$  periods and we suppose that  $\sum_j t_j \leq K.N$ . No precedence constraints are imposed.
- **Ouputs**: We want to schedule the jobs of **J** inside the periods  $1, \ldots, N$ , in such a way that no more than K jobs are performed during a same period *i*.

Then we easily check that any instance of the well-known strongly NP-Complete **Bin Packing** problem (see [20],

[42]) can be polynomialy reduced to an instance of **PVSync-Sched** so that **PVSync-Sched** is also strongly NP-Complete.

### The Battery Level.

Let us consider now the *Battery* level, which means that we suppose that the jobs of J have been scheduled and that we deal with variables  $Y_{j,k}$ , that distribute the batteries among the jobs. We focus on the constraints (E3, E4, E5, E9, E10) of **PVSync**, without taking care of the activity of the PV-Plant, (infinite free production rates  $R_i$ ), and while restricting ourselves to 2 batteries. More precisely, we consider the following restriction **PVSync**:

### **PVSync-Battery**

### - Inputs:

- The period set  $\{1, \ldots, N\}$ .
- The job set  $\mathbf{J} = \{1, \ldots, J\}$ : A job j requires  $e_j$  energy. Every job j has been scheduled inside a single period  $i(j) \in \{1, \ldots, N-1\}$ . We suppose that J = 2.(N-1) and that no more than 2 jobs have been scheduled during a same period.
- Two identical batteries  $k_1, k_2$ , initially loaded with a same energy amount  $H_0$ .
- Outputs: We want to assign the batteries to the jobs in a way that is consistent with the energy requirements.

### Theorem 1: PVSync-Battery is NP-Complete.

**Proof**: We may consider the case when the initial load  $H_0$  is equal to  $\frac{\hat{e}}{2}$  with  $\hat{e} = \sum_j e_j$ . Then we see that for any period *i*, there must exist exactly 2 jobs j(i) and  $\overline{j}(i)$  which are scheduled at period *i*. We may suppose  $e_{\overline{j}(i)} \ge e_{j(i)}$ . It comes that  $k_1$  and  $k_2$  must be active during periods  $1, \ldots, N - 1$  and can only recharge at period *N*. During those periods  $1, \ldots, N - 1$ ,  $k_1$  and  $k_2$  must globally provide the same energy  $\frac{\hat{e}}{2}$ . Thus, solving our problem means partitioning the period set  $1, \ldots, N - 1$  into 2 subsets  $N_1$  and  $N_2$  in such a way that  $\sum_{i \in N_1} (e_{\overline{j}(i)} - e_{j(i)}) = \sum_{i \in N_2} (e_{\overline{j}(i)} - e_{j(i)})$ . We get a reduction to the **2-Partition** problem (see [20], [42]) and we conclude. End-Proof.

# **3.2 Merging the batteries: a projection mechanism**

**PVSync** is a complex problem, with 2 encapsulated decision levels, respectively related to job scheduling and battery assignment, which both involve their own NP-Complete satisfiability sub-problems. The discussion about the variants of **PVSync** and Remark 4 showed that the production level may itself become more complex, even when remaining inside the **P-Time** class. So, even if we work according to the centralized paradigm, dealing with large size or real time constrained instances of

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**PVSync** should push us to find a way to partially bypass some levels and among them the battery level. This trend will of course be reinforced as soon as we address the collaborative issue.

According to this purpose, we shortcut the battery level by merging the K batteries into a unique virtual one. Relaxing this way **PVSync** will later help us in a significant way, when it will come to the design of *job scheduler* oriented algorithms that schedule the jobs while partially bypassing the production issue. More precisely, we start from a **PVSync** instance and perform the following construction:

- We replace the K batteries, by a single macro-battery with storage capacity  $\hat{C} = K.C.$  For any period  $i, \hat{Q}_i$  will mean the energy amount loaded into this macro-battery during period i.
- We forbid more than K jobs to be running during a same period and we impose the *Idle Battery* constraint (E13):
  - For any period *i*,  $\hat{Q}_i \leq C^R.(K-n(Z,i)).$  (E13) This constraint bounds the energy loaded into the jobs without explicitly involving the batteries. It implies that no more than *K* jobs are simultaneously running.

**Remark 5**: The *macro-battery* is completely virtual and can be viewed as a *projection* of batteries onto the job scheduler. It provides us with a way to shortcut the battery level.

This construction leads us to set a relaxation of **PVSync**, denoted by **PVSync-Merge**. In order to analyze the complexity of the *Idle Battery* constraint (E13), let us restrict **PVSync** to 4 periods, unit-period jobs, no temporal constraints, and a PV-Plant activity reduced to energy purchase. More precisely, let us set the following problem **PVSync-Idle**:

### **PVSync-Idle**

- Inputs:
  - The period set  $\{1, 2, 3, 4\}$ .
  - The unit-period job set  $\mathbf{J} = \{1, \dots, J\}$ : A job *j* requires  $e_j$  energy.
  - Battery parameters  $K, C, C^R$ .
- **Ouputs**: We deal with a macro-battery initially loaded with an energy amount  $H_0 = \frac{(\sum_j e_j)}{2}$ , and provided with a storage capacity  $\hat{C} = H_0$ and a recharge capacity coefficient  $C^R = \frac{H_0}{J}$ . This macro-battery can buy energy according infinite purchase costs in periods 1 and 3 and null purchase costs in periods 2, 4. Then we want to schedule under a null cost the jobs of **J** inside the periods  $\{1, 2, 3, 4\}$ , in such a way that:

 The *Idle Battery* constraint is satisfied: For any period *i*,

$$\hat{Q}_i \le C^R.(K-n(Z,i)). \tag{E13}$$

- For any period *i*, the load  $\hat{W}_i$  of the macrobattery at the end of *i* does not exceed  $\hat{C} = H_0$ .

Then we check that solving **PVSync-Idle** means partitioning the job set **J** into 2 subsets  $J_1, J_2$  such that  $\sum_{j \in J_1} e_j = \sum_{j \in J_1} e_j$ . We derive from the NP-Completeness of the 2-Partition (see [20], [42]) problem the NP-Completeness of the **PVSync-Merge** problem.

Of course, both the strong NP-Completeness of **PVSync-Sched** and the NP-Completeness of **PVSync-Idle** imply that **PVSync-Sched** is strongly NP-Hard.

## Extending a Schedule Vector Z into a Feasible Solution of PVSync-Merge

Since the leader object in **PVSync-Merge** is the schedule vector  $Z = (Z_{j,i}, j = 1, ..., J, i = 1, ..., N)$ , we are now going to characterize the conditions which make possible to extend Z into a full feasible solution of **PVSync-Merge**, in a way which does not involve the variables  $U, V, \hat{Q}, W$ . This characterization will help us in dealing with *schedule* vector Z while bypassing the lower levels of **PVSync**. In order to provide it, we need some additional notations:

- For any periods  $i, i_1$ , we set:
  - Conso(i, i<sub>1</sub>, Z) = ∑<sub>j</sub> s.t. i≤Start(Z,j)≤i<sub>1</sub> e<sub>j</sub>. Conso(i, i<sub>1</sub>, Z) means the energy consumption by the jobs which start no sooner than i and no later than i<sub>1</sub>.
  - $ProdMax(i, i_1, Z) = \sum_{i_2 \text{ s.t. } i \leq i_2 \leq i_1} (K n(Z, i_1)).C^R.$  $ProdMax(i, i_1, Z)$  means the maximal energy that the macro-battery may load during periods  $i, \ldots, i_1.$

Then we may state:

**Theorem 2**. Schedule vector Z may be extended into a feasible solution of the **PVSync-Merge** problem if and only if:

- For any period i:  $H_0 + ProdMax(1, i, Z) \ge Conso(1, i + 1, Z).$  (E14)

- For any periods 
$$i, i_1, s.t.$$
  $i \le i_1$ : (E15)  
 $\hat{C} + ProdMax(i, i_1, Z) \ge Conso(i, i_1 + 1, Z)$ .

**Proof**: Above conditions (E14, E15) are clearly necessary: The first one tells us that at any period i, the macrobattery should have received enough energy in order to ensure that any job j starting no later than period i + 1 might be achieved. The second one tells us that, if we consider a sequence of periods  $i, \ldots, i_1$ , then the macro-battery should receive enough energy during those periods in order to achieve all jobs starting no sooner than i and no later than

 $i_1 + 1$ . The key point is about sufficiency. We proceed by induction on *i*, and suppose the converse. We suppose that  $i_1$  is such that we could schedule the production in such a way that all jobs starting no later than  $i_1$  could be achieved, and that at the end of period  $i_1$ , we cannot provide the jobs *j* starting in  $i_1 + 1$  with the energy that they require. We may impose our production strategy to be such that at any period *i*, we load the macro-battery with as much energy as possible, taking into account the *Idle Battery* constraint (E13) and the storage capacity  $\hat{C}$ . Then we see, by moving backward from  $i_1$  to 1, that either we reach some period *i* such that (E15) is violated or we reach period i = 1 in such a way that (E14) is violated. We conclude. **End-Proof** 

## 4 The cooperative issue

There are several way to address this *collaborative* issue. One may adopt the point of view of a specific player, and emulate the interaction that this player is likely to develop with its partners. Another approach consists in keeping on with the centralized paradigm, and supposing that some mediator player fairly distributes costs and profits among the other players. This second point of view corresponds to the *Cooperative Game* theoretical framework. Though our purpose here is to focus on the first approach, we are first going to briefly describe the way **PVSync** may be cast into the *Cooperative Game* framework.

### 4.1 A cooperative *PVSync* game

Let us recall that a *cooperative game*  $(\Omega, Val)$  (see [33], [21]) is defined as a set of players  $\Omega$  and a function Valwhich, to any subset A of  $\Omega$ , called *coalition* makes correspond its *cost* value Val(A). Then the problem becomes to fairly distribute the cost  $Val(\Omega)$  among the players, in such a way that no coalition is tempted to leave the game. Several approaches may be tried. The most popular one is related to the *core* notion: a price vector  $\pi = (\pi_{\omega}, \omega \in \Omega)$ is in the core of the game  $(\Omega, Val)$  iff:

- $-\sum_{\omega}\pi_{\omega}=Val(\Omega)$
- For any coalition A,  $\sum_{\omega} \pi_{\omega} \leq Val(A)$

This core may be empty, which imposes trying weaker ways to distribute the cost  $Val(\Omega)$  among the players, for instance according to the Shapley values. Conversely, it may contain too many elements, which leads to more restrictive notions such as the *Nucleolus* (see [7],[33]).

In the present case we suppose, for the sake of simplicity, that every job j is identified with exactly one player, and that the players are independent. This implies that no precedence relation << is imposed to the jobs, since such a constraint would induce a dependence between related players. Then we define a cooperative game *G-PVSync* by setting:

 Val(A) = PVSync(J)-PVSync(J – A). Val(A) represents the marginal cost induced by the jobs of A with respect to PVSync(J).

Then we may state:

**Theorem 3**: If all sale prices  $S_i$  are null, then the core of *G*-PVSync is not empty.

**Proof**: Let us recall that Bondareva/Shapley Theorem (see [8]) provides us with a characterization of the nonemptiness of the core of a cooperative game  $(\Omega, Val)$ . This characterization comes as follows:

- A non negative vector μ = (μ<sub>A</sub>, A ⊆ Ω) is said to be balanced, if, for any player ω, ∑<sub>A s.t. ω∈A</sub> μ<sub>A</sub> = 1.
- Then the cooperative game  $(\Omega, Val)$  has a nonempty core if and only if for any balanced vector  $\mu$ ,  $Val(\Omega) \leq \sum_{A} \mu_{A} Val(A)$ . (E16)

So let us consider some balanced vector  $\mu$  together with some optimal solution Sol = (X, Y, Z, T, U, V, W, Q) of **PVSync**. Let us set  $\overline{\mu} = \sum_A \mu_A$ . (E16) requires:  $PVSync(\{1, \ldots, J\}) \leq \sum_A \mu_A (PVSync(\{1, \ldots, J\}))$  $-PVSync(\{1, \ldots, J\} - A))$ . This equality is equivalent to:  $\sum_A PVSync(\{1, \ldots, J\} - A) \leq (\overline{\mu} - 1).PVSync(\{1, \ldots, J\})$ . So we only need to check that it is possible to decompose

 $(\overline{\mu} - 1)$ . Sol into a non negative linear combination  $\sum_{A} \mu_A.Sol(\{1, \ldots, J\} - A)$ , where every vector  $\overline{Sol}(\{1,\ldots,J\} - A)$  is a feasible solution of the restriction of **PVSync** to the jobs of  $(\{1, \ldots, J\} - A)$ . If we can do it, then we conclude since every value  $PVSync(\{1,\ldots,J\} - A)$  is going to be no larger than the cost of  $Sol(\{1, \ldots, J\} - A)$ . Getting such a decomposition can be done by tracking inside Sol, for every job j, the energy consumed by j and the energy produced in order to match this consumption. As a matter of fact, we might also represent the way energy circulates according to (U, V, W, Q) as a flow vector in a network derived from the periods and the batteries involved in PVSync (time expanded network) and decompose it along the jobs of J into a multi-commodity flow vector (see [2], [9]). This process makes appear, for every battery k, the useless energy  $C^{Res}(k)$  remaining inside k throughout the whole time space. It yields a decomposition of Sol as Sol =  $\sum_{j} SolJob_{j}$ , where every partial solution  $SolJob_j$  meets reduced capacities  $C - C^{Res}(k), k = 1, ..., K$ . Then  $Sol(\{1, ..., J\} - A)$  comes as  $\sum_{j \in \{1,...,J\}-A} SolJobt_j$ . End-Proof

**Remark 6**: If we allow non-null sale price, then we may check that above reasoning does not hold anymore.

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# 4.2 The job scheduler/PV-Plant interaction: surrogate estimators

We now address the collaborative issue while adopting the point of view of the job scheduler and trying to emulate the interaction that this player is likely to develop with its partner. This point of view corresponds to the most natural bi-level setting of PVSync. According to it, we rely on a surrogate estimator SurrPVCost, which with any schedule vector Z consistent with (E5, E12), and any value of some flexible parameter vector  $\gamma$ , associates an estimation  $SurrPVCost(Z, \gamma)$  of the value RestrictPVSync(Z). The role of the parameter  $\gamma$  is to introduce flexibility in order to mitigate the fact that  $SurrPVCost(Z, \gamma)$  provides us with no more than an approximation of RestrictPVSync(Z). The effective value of  $\gamma$  will be tuned all along the interaction process, in such a way that this process converges to a consensual solution. So, at every step during this process, we shall compute Z while restricting ourselves to contraints (E5, E12) together with some additional (surrogate) constraints  $Cons(\gamma, Z)$ . Those surrogate constraints will aim at both avoiding **Restrict-PVSync**(Z) to be unfeasible and at providing a container for the interaction between the job scheduler and its partner. We shall perform this computation of Z in such a way that it minimizes the cost  $\alpha.(\sum_{j,i} i.Z_{j,i}) + SurrPVCost(Z, \gamma)$ . Taken as a whole, this interaction will proceed as follows (see Fig. 4):

### Collaborative algorithmic scheme

Initialize  $\gamma$  and constraints  $Cons(\gamma, Z)$  about schedule vector Z and  $\gamma$ ;

Set the initial proposal of the job scheduler: Compute Z which minimizes  $\alpha.(\sum_{j,i} i.Z_{j,i}) + SurrPVCost(Z, \gamma)$  while meeting (E5, E12) and  $Cons(\gamma, Z)$ ;

While Not Stop do

- 1. Set the counter-proposal from the PV-Plant: Solve **Restrict-PVSync**(Z) and retrieve new constraints to insert into  $Cons(\gamma, Z)$ ;
- 2. Update Stop; If Not Stop then

Update  $\gamma$ ;

Set the new proposal of the job scheduler: Compute Z minimizing  $\alpha$ .  $\sum_{j,i} i.Z_{j,i} + SurrPVCost(Z, \gamma)$  while meeting (E5, E12) and updated  $Cons(\gamma, Z)$ ;

Retrieve the best schedule vector Z obtained this way.

Of course, this heuristic management of **PVSync** may also be applied under the standard *centralized* paradigm approach in the case of large size instance or real time requirements.



Figure 4: A collaborative scheme

### 4.3 Surrogate estimators and constraints

We distinguish the surrogate estimator  $SurrPVCost(Z, \gamma)$  from the additional constraints  $Cons(\gamma, Z)$ .

**Remark 7**: Notice, in the case of the surrogate estimator  $SurrPVCost(Z, \gamma)$ , that it does not really aim at providing an approximation in the standard sense of RestrictPVSync(Z), rather at efficiently driving above collaborative algorithmic scheme towards good solutions.

### 4.3.1 Surrogate constraints

Previous Section 3 leads us to insert (E14) and (E15) into  $Cons(\gamma, Z)$ . Still, though these constraints ensure the feasibility of the **PVSync-Merge** problem of Section 3, they may not be sufficient in the case of the full **PVSync** problem. Typically, if 2 jobs  $j_1$  and  $j_2$  such that  $e_{j_1} = e_{j_2} = 10$ , are scheduled to start at period 1, if K = 2 and if  $H_{k_1}^{Init} = 5$ ,  $H_{k_2}^{Init} = 15$ , then we cannot successfully assign the batteries to the jobs, while we may extend this schedule into a feasible solution of **PVSync-Merge**.

In order to reinforce (E14, E15), we proceed in a heuristic way, while relying on the flexible vector  $\gamma$ :

- We first set, for any energy amount  $E : m(E) = \lceil \frac{E}{C^R} \rceil$ . This number m(E) means the number of consecutive periods necessary in order to load a battery with E energy. Let also recall that  $L(Z, i_1)$  denotes the number of idle batteries induced by Z at period i.
- Then we impose the following parametric heuristic constraints, which depend on flexible parameters  $\gamma_0$  and  $\gamma_1$ :
  - For any period *i*, let  $j_1, \ldots, j_S$  be the jobs scheduled to start at period i + 1 according to schedule vector *Z*. Then, for any  $i_1 \le i$ , we impose: (E18)  $L(Z, i_1) \ge \sum_{i_1 \le i_2 \le i_3 \le i_4} \sum_{j_1 \le j_2 \le j_3 \le j_4} \sum_{i_1 \le i_4 \le i_4} \sum_{j_1 \le j_2 \le j_4} \sum_{j_1 \le j_4 \le j_4} \sum_{j_4 \le j_4}$

$$\gamma_0.|\{s \text{ s.t. } m(e_s \ge (i-i_1+1))\}|.$$

- For any period *i*, let us denote by  $j_1, \ldots, j_S$  the jobs starting at i + 1, ordered according to decreasing  $m(e_{j_s})$  values, and by  $S_1 \leq S$  the largest *s* value such that  $m(e_{j_{S_1}}) \geq i$ . Then we impose that there exist  $k_1, \ldots, k_{S_1}$  in **K** such that for any  $s \leq S_1$ :  $HInit_{k_s} + i.C^R \geq \gamma_1.e_{j_s}$ . (E19) Constraints (E18, E19) aims at making in such a way that at any period i, there should exist batteries which have been idle for enough time in order to feed jobs starting in i + 1.

### 4.3.2 A price based surrogate estimator

We proceed here in an empirical way, while following the idea that the production cost induced by a schedule vector Z is determined by the distribution of values  $L(Z, i), i \in \{1, \ldots, N\}$ . This suggests us to express the surrogate cost  $SurrPVCost(Z, \gamma)$  as a sum  $\sum_{i} \prod_{i,L(Z,i)}$ , where  $\prod_{i,L}$  is an estimation of the cost induced by L batteries in recharge (idle) at period i. According to this idea, we first make appear a *standard production price*  $\prod_{i,L}^{Stand}$  which, with any idle battery number L and any period i, associates a kind of a reference price of the recharge of L batteries at period i. We do it by noticing that if all batteries receive a same charge  $E^{Mean}$  at every period when they are idle, then the production cost Cost should be equal to  $\sum_{i} \prod_{i,L(Z,i)}^{Stand}$ . So we derive *standard production prices*  $\prod_{i,L}^{Stand}$  as follows:

$$\Pi_{i,L}^{Stand} = P_i (L.E^{Mean} - R_i) \text{ if } L.E^{Mean} \ge R_i \text{ and } \\ \Pi_{i,L}^{Stand} = S_i (L.E^{Mean} - R_i) \text{ else.}$$

In order to flexibilize those prices, we follow intuition which tells us:

- If  $L(Z, i).E^{Mean} \ge R_i$ , then  $\Pi_{i,L}$  should increase with  $P_i$ ;
- If  $L(Z, i).E^{Mean} \leq R_i$ , then  $\Pi_{i,L}$  should decrease (negative cost) as  $S_i$  increases.

This leads us to introduce 2 components  $\gamma_2$  and  $\gamma_3$  of flexible parameter  $\gamma$  and to set:

$$- \Pi_{i,L} = \Pi_{i,L}^{Stand} (1 + \gamma_2 (P_i - P^{Mean}))$$
 if   
 
$$L(Z, i) \cdot E^{Mean} \ge R_i,$$

$$- \Pi_{i,L} = \Pi_{i,L}^{Stand} . (1 + \gamma_3 . (S_i - S^{Mean}))$$
 else.

### 4.3.3 A machine learning based surrogate estimator

Instead of relying on energy price coefficients  $\Pi_{i,L}$  we use a neural network CNN\_PVSync in order to provide us with the quality of a scheduled vector Z. Network CNN PVSync involves 467 synaptic coefficients and is trained with 9000  $\mathbf{PVSync}(Z)$  instances, among them 8110 training instances and 890 validation instances, solved with the MILP model of Section 2. This small ratio of 1/20 between the number of synaptic coefficients and the number of training instances eases the training process (stochastic gradient optimization process), making the error gap evolve in a monotonic way along the epochs and stabilize itself in a natural way in the neighborhood of some optimal error gap. The stochastic gradient algorithm behaves as if it were dealing with a standard optimization problem, with a small number of variables and an objective function defined by an average violation of a larger set of constraints. A consequence is that we do not need to

observe the evolution of the error gap along the epochs in order to identify the epoch that induces the best error gap.

CNN PVSync is designed as a convolutional neural network (CNN). CNNs have been mostly used for 2D-pattern recognition, since images are very large size inputs and since the convolutional masks are well-fitted to the recognition of local patterns. In the present case, our goal here is to learn the optimal value of a combinatorial optimization problem (the optimal cost related to the production sub-problem induced by fixing the decision of the job scheduler), in order to drive a heuristic scheduling process. An important feature of a CNN is that, at the contrary of most neural networks, it can deal with flexible inputs of different sizes. It is our case here, since the size of our target combinatorial optimization problem may vary. That is why we choose to work with a CNN. Notice that the error gap induced by the the CNN is not at stake here, rather its ability to drive the heuristic algorithm toward good solutions.

A convolutional network usually works in 3 steps. In the first step a same standard *perceptron* CM, called convolutional mask, is applied to fixed size segments of the input vector  $IN = (IN_m, m \in \{1, \dots, M\}),$ where M is the variable size of the input data vector. This perceptron CM yields an output vector  $OUT = (OUT_m, m \in \{1, \dots, M\})$ , with the same size as IN. In the next step, a pooling mechanism is applied to OUT, in order to compact it into the fixed size input vector  $\overline{IN}$  of another perceptron NPool. In the last step, NPool turns  $\overline{IN}$  into the final output  $\overline{OUT}$  of CNN. In the present case the final output of CN PVSync is a number  $\theta$  between 0 and 1. This number refers to the formulation of the optimal value RestrictPVSync(Z)as a barycentric combination LowPVSync(Z) +  $\theta.(UpPVSync(Z))$ - LowPVSync(Z)), where UpPVSync(Z) and LowPVSync(Z) are respectively an upper bound and a lower bound of RestrictPVSync(Z). In case RestrictPVSync(Z) does not exist, that means in case PVSync(Z) is not feasible, we do as if RestrictPVSync(Z) were equal to UpPVSync(Z)(then  $\theta$  should be equal to 1). Figure 5 shows the architecture of CNN PVSync whose main components come as follows:

- Input layer: We homogenize any input  $(Z, P, S, R, H^{Init}, C, C^R, K)$  of **Restrict-PVSync**(Z) as a 7(N + 1) vector IN, with  $IN[i] = (\overline{P}_i, \overline{S}_i, \overline{R}_i, \overline{\mu}_i, \overline{L}_i, \overline{C}, \overline{C^R})$ , given by:
  - $\overline{P}_i = \frac{P_i}{P^{Mean}}; \overline{S}_i = \frac{S_i}{P^{Mean}}.$
  - $\mu_i = \sum_{\substack{j \text{ active at period } i}} e_j^{Mean}; \mu_0 = 0;$  $\overline{\mu}_i = \frac{\mu_i}{R^{Mean}}$ . This last quantity  $\overline{\mu}_i$  identifies the normalized amount of energy consumed at any period.
  - $\overline{R}_i = \frac{R_i}{R^{Mean}}; \overline{R_0} = \frac{\sum_k H_k^{Init}}{R^{Mean}}.$



Figure 5: The neural network CNN PVSync

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$$\overline{L}_i = \frac{L(Z,i)}{K}; \overline{C} = \frac{C}{R^{Mean}}; \overline{C^R} = \frac{C^R}{R^{Mean}}.$$

- Convolutional Mask: CM works on any vector  $IN_i^* = (IN[i], \dots, IN[i+4])$ , which means an input with 35 input arcs. It contains 3 inner layers, respectively of sizes 8, 4 and 2, and ends into an output layer, that yields 1 input value  $OUT_i$ . This network is complete in the sense that all 322 inner synaptic arcs are allowed, together with standard biased sigmoid activation functions  $x \to \frac{1}{1+exp(-kx)}$ , with parameter k. Thus the number of synaptic coefficients related to this convolutional mask is 320 + 35 = 355.
- The pooling Mechanism: It works by merging consecutive values  $OUT_i$  into a single one, in such a way that we get an intermediate vector IN, with 13 entries, all with values between 0 and 1.
- The Final Perceptron NPool: Once the pooling mechanism has been applied, we handle resulting 13 dimensional vector  $\overline{IN}$  with a perceptron NPool, with input layer of size 13, intermediate layers of size 6 and 3, and a final layer of size 1. This network is complete in the sense that all 99 inner synaptic arcs are allowed, together with standard biased sigmoid activation functions  $x \rightarrow \frac{1}{1+exp(-kx)}$ , parameter k being provided with the same value as in the convolutional mask. Thus, the number of synaptic coefficients associated with this final perceptron is 13 +99 = 112.

Taken as a whole, CNN PVSync involves 467 synaptic coefficients.

**Outputs of** CNN PVSync: As previously told, the concatenation of CM and NPool yields a value  $\overline{OUT} = \theta$  between 0 and 1, which refers to the barycentric setting:

RestrictPVSync(Z)= LowPVSync(Z) + $\theta.(UpPVSync(Z) - LowPVSync(Z)),$ 

where UpPVSync(Z) and LowPVSync(Z) are respectively an upper bound and a lower bound of RestrictPVSync(Z), computed as follows:

- $LowPVSync(Z) = -\sum_{i} S_i.R_i.$   $UpPVSync(Z) = (Sup_iP_i).(\sum_{j} e_j) (\sum_{i} S_i.R_i).$

In case **Restrict-PVSync**(Z) is unfeasible, we do as if RestrictPVSync(Z) were equal to UpPVSync(Z), that means is if  $\theta$  were supposed to be equal to 1.

The way we train the network CNN\_PVSync in order to make it learn its synaptic coefficients will be described in the next section 5, devoted to numerical experiments.

### 4.4 Job scheduler oriented heuristics for the search for schedule vector Z

Dealing with a blackbox objective function such that CNN PVSync can only be done through a heuristic scheme. So we design a simple job scheduler oriented heuristic SurrPVCost that works in 2 steps and that we may adapt to both the price based version and the machine learning version of the SurrPVCost estimator.

### SurrPVCost Job Scheduler Oriented Algorithm

- Initialization : Pick up the jobs j according to increasing  $Min_i$  values (updated through constraint propagation) and assign them starting periods which maintain constraints (E5, E12, E14, E15, E17, E18, E19), meet time windows and the precedence constraints, and minimize  $\alpha . (\sum_{j,i} i.Z_{j,i}) + SurrPVCost(Z, \gamma);$
- While Not Stop do : Remove some job j from the current schedule and reinsert it (while possibly delaying other jobs) in such a way that  $\alpha (\sum_{j,i} i Z_{j,i}) +$  $SurrPVCost(Z, \gamma)$  decreases.

#### 5 Numerical experiments

**Purpose**: We want to evaluate the behavior of the *job* scheduler oriented heuristic SurrPVCost, implemented along the two surrogate estimators described in sections 4.3.2 and 4.3.3, and its ability to yield under small computational costs a good approximation of the optimal value of PV-Sync. According to this purpose, the MILP formulation of PV-Sync is used only in order to provide us with benchmark results.

**Technical Context**: We use a processor IntelCore i5-6700@3.20 GHz, with 16 Gb RAM, together with a C++ compiler, Linux as O.S. libraries CPLEX20.1 (for ILP models) and TensorFlow/Keras (for machine learning).

**Instances**: As for the PV-Plant side, we generate 2 integers M and N, N being a multiple of M, with  $N = 10, \ldots, 40, M = 2, \ldots, 5$ . Then we split the period set into M macro-periods, corresponding to different mean production rates and prices. Related coefficients  $R_i, P_i, S_i$  are generated accordingly. Introducing those macro-periods provides us with realistic prices and production levels that may be related to human activity and to the weather.

As for the scheduling part, we try to both ensure feasibility and put stress on the instances. So we generate J, together with mean duration and mean energy coefficients  $t^{Mean}$ and  $E^{Mean}$ . We set  $C = 2.Sup_j \ e_j$  and  $K = \lambda.J.(\frac{t^{Mean}}{N})$ , where  $\lambda$  is some control parameter. For any  $k = 1, \ldots, K$ , we generate  $H_k^{Init}$  between  $\frac{C}{3}$  and C. In order to make the PV production match the demand, we update the  $R_i$ by doing in such a way that  $\sum_i R_i = \tau.J.C, \tau$  being a control parameter with value between 0.5 and 2. Finally we generate the key parameter  $C^R$  in such a way that batteries globally receive at least  $\beta.J.C$  energy units during the whole process,  $\beta$  being a control parameter with value between 1.5 and 4. So the main parameters of an instance are: N = Period Number, J = Job Number, M = Macro-period Number, K = Battery Number,  $t^{Mean}$ = Mean Job Length,  $\alpha = Time$  versus Money Value,  $\beta =$ Recharge Stress Value,  $\tau = Production$  Stress.

According to this, we generate 10 groups of instances, every instance group  $G_Id$  containing 30 instances consistent with the characteristics N, J, M,  $t^{Mean}$ , K,  $\alpha$ ,  $\beta$ ,  $\tau$  described in the following table 3.

Table 3: Instance group characteristics

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$G_Id$	N	J	M	$t^{Mean}$	K	$\alpha$	$\beta$	au
1	40	21	3	4	4	1	2	0,5
2	40	23	4	5	4	0,5	3	1
3	40	20	5	6	5	0,2	4	2
4	40	24	3	4	5	1	2	0,5
5	40	32	4	6	4	0,5	3	1
6	40	34	5	8	4	0,2	4	2
7	60	43	4	5	3	1	3	1
8	60	47	6	10	3	0,5	4	2
9	60	53	4	5	5	1	3	1
10	60	61	6	10	5	0,5	4	2

# 5.1 Training the neural network CNN PVSync.

For every group instance  $G_Id$  described above and for every instance Id in  $G_Id$ , we randomly generate 30 schedule vectors Z, which meet the constraints (E5, E12, E14, E15, E17, E18, E19). We do it by turning the initialization procedure of the SurrPVCost Algorithm into a partial enumeration procedure, in such a way it can randomly generate several vectors Z meeting constraints (E5, E12, E14, E15, E17, E18, E19). Notice that those vectors may not be extended into a feasible solution of PVSync and that in such a case we consider that RestrictPVSync(Z)is equal to UpPVSync(Z), requiring related value  $\theta$  to be equal to 1. Then we split resulting set of 9000 instances between a training set of 8110 instances and a validation set of 890 instances. The high ratio of 20 between the number of instances and the number of synaptic coefficients significantly eases the training process, making the error gap evolve in a monotonic way until stabilizing itself in a natural way around some approximation of the optimal error gap. We perform the training process while testing 12 sets Hy of hyperparameters, described in the following Table 4. Those hyperparameters are the parameter k of the sigmoid activation function, the batch size Ba, the number of epochs Ep, the loss formula Los(among MS = Mean Square Error, MA = Mean Absolute Error, MSL = Mean Square Logarithmic Error), the optimizer Op (among Ad = Adam, Nad = Nadam, Amx= Adamax, RMS = RMSprop). This table also makes appear, for every hyperparameter set Hy, the gaps (in %) between RestrictPVSync(Z) and  $CNN_PVSync(Z)$ , computed by referring to the value  $\theta$ . Gap T means here the value (in %) of this gap related to the training instance, and Gap V means the same value (in %) related to the validation instances.

Table 4: hyperparameter sets

				21 1			
Hy	k	Ba	Ep	Los	Op	$Gap_T$	$Gap_V$
1	1	2	30	MS	Ad	9.6	12.9
2	0.5	4	30	MS	Ad	11.2	14.8
3	2	1	30	MS	Ad	9.4	12.1
4	3	2	30	MS	Amx	10.5	14.0
5	1.5	4	30	MS	Nad	8.6	11.3
6	2.5	8	30	MS	RMS	9.1	12.5
7	1.5	4	50	MA	Ad	8.7	11.8
8	1.5	4	50	MA	Ad	8.1	11.0
9	1.5	4	50	MSL	Ad	8.4	11.2
10	1.5	2	50	MSL	Nad	8.7	11.9
11	1.5	4	50	MA	Amx	10.9	14.7
12	1.5	8	50	MS	RMS	8.3	11.1

**Comments:** The best gap between RestrictPVSync(Z) and  $CNN_PVSync(Z)$  corresponds to Hy = 8, with value a little bit larger than 8% for the training instances and 11% for the validation instances. Recall that this error gap is not really at stake, rather the ability of  $CNN_PVSync(Z)$  to drive the heuristic *job scheduler* oriented *SurrPVCost* algorithm towards satisfactory solutions.

## 5.2 Evaluating the heuristic management (*job scheduler* oriented algorithm *SurrPVCost* of Section 4.4) of the PVSync problem through surrogate components

For any instance group  $G_Id$  described in Table 3, we generate exactly one instance Id and, for every such instance:

- We apply the CPLEX12 library (Table 5) to the **PVSync\_MILP** model. Then we get (in less than 1 CPU h), a lower bound *LB*, an upper bound *UB* and CPU time *T\_MILP*.
- We apply (Table 6) the *job scheduler* oriented algorithm *SurrPVCost* of Section 4.4 while relying on the pricing mechanism described in Section 4.3.2 and setting Π<sub>i,L</sub> = Π<sup>Stand</sup><sub>i,L</sub> for any *i*, *L*. We denote by *PR*1 resulting **PVSync** value. We do the same (Table 6) with 8 combinations of γ values and denote by *PR*8 resulting value. We provide the CPU times *T\_PR*8 (in seconds) required by the scheduling heuristic *SurrPV-Cost* described in Section 4.4.
- We apply (Table 7) the *job scheduler* oriented algorithm *SurrPVCost* of Section 4.4 while relying on the machine learning estimator described in Section 4.3.3 and denote by *ML* related value. We provide the CPU times *T\_ML* required by the *SurrPVCost job scheduler* oriented algorithm described in Section 4.4.

Those results may be summarized into the following tables:

Table 5.	Behavior	of the	PVSvnc	MILP	model
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Id	LB	UB	$T\_MILP$
1	- 239.64	- 235.91	3600
2	- 85.56	- 82.47	3600
3	- 1439.38	- 1311.60	3600
4	488.45	619.15	3600
5	212.90	248.33	3600
6	177.46	198.35	3600
7	1738.56	1760.33	3600
8	Fail	Fail	Fail
9	571.31	3742.10	3600
10	- 52.92	155.27	3600

**Comments**: As expected, the global ILP model is in trouble, even on small instances. We notice that we may get negative cost values, because of the sales. This makes difficult reasoning in terms of percentages. Still, for small J, UB looks close to optimality.

In case the *job scheduler* oriented heuristic *SurrPVCost* relies on the parametric pricing mechanism described in Section 4.3.2, it seems to be rather efficient. Though it only relies on a heuristic *SurrPVCost* algorithm for the computation of schedule vector Z, it yields better results than the MILP model in the 3 instances with largest sizes. Its

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139.68

478.62

	Table 0. Denavior of the pricing scheme							
Id	UB	PR1	PR8	$T\_PR8$				
1	- 235.91	- 216.68	- 216.68	48.22				
2	- 82.47	- 75.84	- 78.52	71.83				
3	- 1311.60	- 1165.59	- 1208.45	76.82				
4	619.15	659.07	659.07	62.64				
5	248.33	406.56	327.05	131.83				
6	198.35	221.16	200.04	83.49				
7	1760.33	1971.18	1904.09	579.50				
8	Fail	- 397.6	- 397.6	1000,6				
9	3742.10	1267.59	1267.59	1008.17				

Table 6: Behavior of the pricing scheme

Table 7:	Behavior	of machine	learning

167.52

	fuote /: Benavior of machine feating							
Id	UB	ML	$T_ML(s)$					
1	- 235.91	- 193.38	10.85					
2	- 82.47	- 50.08	21.28					
3	- 1311.60	- 890.00	28.60					
4	619.15	766.79	15.50					
5	248.33	398.20	45.60					
6	198.35	254.06	25.08					
7	1760.33	1861.24	72.25					
8	Fail	- 359.07	105.10					
9	3742.10	1548.25	180.05					
10	155.27	199.00	80.05					

sensitivity to parameter  $\gamma$  does not look very significant: In 4 cases, the best result is obtained with standard prices  $\Pi_{i,L} = \Pi_{i,L}^{Stand}$  for any *i*, *L*. In case we apply *SurrPVCost* algorithm while relying on the machine learning oriented estimator described in Section 4.3.3, we see that the gap between *UB* and *ML* is more important. Yet, this second approach offers more genericity features than the first one.

## 6 Conclusion

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155.27

We dealt here with a complex scheduling problem, involving encapsulated resources and synchronization mechanisms. Since handling it as a whole is difficult and may not fit collaborative contexts, we shortcut the resource production sub-problem and replaced it by a parametric surrogate estimator. We tried 2 approaches: the first one relied on artificial prices; the second one on a neural network. Numerical experiments made appear, at least in our case, a better efficiency of the first approach. Still, because of the genericity of machine learning, a priori better fitted for the management of the uncertainty inherent to our problem, it would be worthwhile to try to go deeper with it. Those two points will be the backbone of a future research.

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